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The weberite structure  $(A_2B_2X_7)$  is an anion-deficient fluoriterelated superstructure. Compared with fluorites, the reduction in the number of anions leads to a decrease in the coordination number of the *B* cations (VI coordination) with respect to the *A* cations (VIII coordination), thus allowing the accommodation of diverse cations. As a result, weberite compounds have a broad range of chemical and physical properties and great technological potential. This article summarizes the structural features of weberite and describes the structure in several different ways. This is the first time that the stacking vector and stacking angle are used to represent the weberite structure. This paper also discusses the crystallographic relationship between weberite, fluorite and pyrochlore (another fluorite-related structure). The cation

**Complex ceramic structures. I. Weberites** 

lographic relationship between weberite, fluorite and pyrochlore (another fluorite-related structure). The cation sublattices of weberite and pyrochlore are correlated by an axial transformation. It has been shown that the different coordination environment of anions is due to the alternating layering of the  $AB_3$  and  $A_3B$  close-packed cation layers. A stability field of weberite oxides is proposed in terms of the ratio of ionic radius of cations and relative bond ionicity. In addition, a selection of weberite compounds with interesting

# 1. Introduction

properties is discussed.

The weberite crystal structure (space group: *Imma*, No. 74), with typical stoichiometry  $A_2B_2X_7$  (*A* and *B* are cations, *X* is an anion, O or F), is a type of anion-deficient fluorite superstructure ( $AX_2$ ). While several other compounds possess the same stoichiometry (pyrochlores, layered perovskites *etc.*), weberites are isomorphic with the mineral Na<sub>2</sub>MgAlF<sub>7</sub>. This mineral was originally found in Ivigtut in southwestern Greenland and was named after Theobald Weber (Bogvad, 1938). In 1944, Byström (1944) determined the crystal structure, basing his studies on the pyrochlore structure, which is another fluorite-related superstructure.

While the structure has a cationic sublattice arrangement similar to that found in the fluorite structure (face-centered cube), owing to distortions in the anion sublattice, the crystal structure has a high potential to accommodate diverse metals. The cations in (011) planes have nearly the same symmetry as in the hexagonal tungsten bronze (HTB) structure. In addition, the triangular network in  $Na_2B^{2+}B^{3+}F_7$  weberites, which is formed by  $B^{2+}$  and  $B^{3+}$  cations in the HTB-like planes, potentially supports various magnetically ordered systems. To date, fluorine-based weberites such as  $Na_2B^{2+}B^{3+}F_7$  and  $Ag_2B^{2+}B^{3+}F_7$  have attracted most of the attention owing to their interesting magnetic properties (Cosier *et al.*, 1970; Dance *et al.*, 1974; Frenzen *et al.*, 1992; Laligant *et al.*, 1989; Laligant, Ferey *et al.*, 1987; Pankhurst *et al.*, 1991; Ruchaud *et* 

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			Atomic position					
Atoms	Wyckoff position	Site symmetry	x	у	z			
<i>A</i> 1	4 <i>d</i>	2/ <i>m</i>	0.25	0.25	0.75			
A2	4a	2/m	0	0	0			
<i>B</i> 1	4c	2/m	0.25	0.25	0.25			
<i>B</i> 2	4b	2/m	0	0	0.5			
X1	8h	т	0	$y_1$	$z_1$			
X2	16 <i>j</i>	1	$x_2$	y <sub>2</sub>	$z_2$			
X3	4 <i>e</i>	mm2	0	0.25	$Z_3$			

 Table 1

 Weberite structure data (origin at A cations) in space group Imma.

X1 is at the center of  $A_3B$ , X2 is in the  $A_2B_2$  tetrahedron and X3 is inside  $A_4B_2$ .

al., 1992; Thompson et al., 1992; Tressaud et al., 1974; Heger, 1973). Investigations on  $A_2B_2O_7$  weberites have mainly focused on crystallography because of the close relationship between the weberite and the pyrochlore structures (Cordfunke & Ijdo, 1988; Groen & Ijdo, 1988; Klein et al., 2006; Reading et al., 2002; Astafev et al., 1985; Bonazzi & Bindi, 2007; Desgardin et al., 1976; Grey et al., 2001, 2003; Grey & Roth, 2000; Ivanov & Zavodnik, 1990). Both of the structures form three-dimensional  $BX_6$  networks and HTB-like layers. Some compounds, for example Ca<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub>, can form a metastable pyrochlore phase, which can be converted into the weberite structure by heating above 973 K (Brisse et al., 1972). Recently, weberite oxides and weberite-related oxides have been reported to possess interesting physical properties (ferroelectric, dielectric and magnetic) as well as photocatalytic activity (Wakeshima et al., 2004; Abe et al., 2004, 2006; Cai & Nino, 2007; Cai et al., 2007; Cava et al., 1998; Ebbinghaus et al., 2005; Ivanov et al., 1998; Grey et al., 2001; Lin et al., 2006; Khalifah et al., 1999; Nishimine et al., 2004, 2005; Plaisier et al., 2002; Wakeshima & Hinatsu, 2006; Hinatsu et al., 2004; Harada & Hinatsu, 2002, 2001; Lam et al., 2003; Wiss et al., 2000; Wltschek et al., 1996; Gemmill et al., 2005).

There are a considerable number of publications on weberite ceramics. However, information on weberites is scattered. While presenting their work on the structure determination of Na<sub>2</sub>Fe<sub>2</sub>F<sub>7</sub>, Yakubovich et al. (1993) devoted more than half of the paper to a comparison of different types of weberite structures in  $Na_2B^{2+}B^{3+}F_7$  compounds and their relationship to the fluorite and the pyrochlore structures, but their discussion was limited to the crystallographic aspects. Lopatin et al. (1985) and Sych et al. (Sych, Kabanova, Garbuz et al., 1988) focused on the stability-field region of these compounds. However, there is no article that correlates the structure and properties of weberites. Therefore, this paper is intended to provide a discussion of weberite ceramics, covering crystallographic aspects including the relationship between weberite, fluorite and pyrochlore, their stability field with respect to pyrochlore, and their interesting properties.

In §2 the structural features of weberite and the characteristics of weberite-like structures are discussed. Several different descriptions of the structure are given and a stacking vector and stacking angle are used for the first time to represent the weberite structure. The crystallographic relationship between the fluorite and the pyrochlore structures is also discussed. It is also shown that the cation sublattices of pyrochlores can be transformed to the weberite-like lattice. The different stacking of neighboring  $AB_3$  and  $A_3B$  layers lead to the different coordination environments of anions in weberite and pyrochlore. A stability field is developed to predict the formation of pyrochlore and weberite oxides. In §3 ferroelectric and dielectric properties of some weberite compounds are discussed.

# 2. Crystal structure

## 2.1. Classic orthorhombic weberite

The space group of the orthorhombic weberite structure is Imma (No.74) with four formula units per unit cell (Z = 4). However, the correct space group of weberites was a subject of controversy for a long time, as it was described as both Imma and Imm2 (Sych, Kabanova & Andreeva, 1988; Haegele et al., 1978; Giuseppetti & Tadini, 1978; Knop et al., 1982; Byström, 1944). The detailed history of the determination of the space group has been reported by Yakubovich et al. (1993). The two space groups are closely related as Imm2 is a subgroup of Imma. The only evidence ruling out Imma was the observation of very weak (*hk*0) with h = 2n + 1 reflections. It was later proven that the existence of (hk0) with h = 2n + 1 reflections from Na<sub>2</sub>NiFeF<sub>7</sub> single crystals and Na<sub>2</sub>NiAlF<sub>7</sub> originated from the Renninger effect ('double reflection' process; Schmidt et al., 1992; Laligant et al., 1989). Thus, there is no doubt that the true space group of the orthorhombic weberite is Imma. The atomic positions and site symmetry are given in Table 1.

In weberites the A ions sit in the 4a and 4d atomic positions with site symmetry 2/m and establish a coordination number of 8 with the anions. The A ions have two different coordination environments. The A1 cations (in atomic position 4d) lie in a highly distorted cube (or square prism) where there are two different A1-X bond lengths. The cubes are edge-shared to form a series of chains in the [100] direction. The A2 cations (in atomic position 4a) are located within bi-hexagonal pyramids in which anions are spaced at three different distances from the central cations. Each pyramid is corner-shared with two other pyramids and edge-shared with four  $A1X_8$  cubes. As presented in Table 1 there are three Wyckoff positions for anions (X1 at 8h, X2 at 16j and X3 at 4e). A1 ions only connect to X1 and X2, while A2 link to all three types of anions (two X1, four X2 and two X3).

The *B* ions are located in the 4*b* and 4*c* Wyckoff positions (site symmetry 2/*m*) and have a coordination number of 6, *i.e.*  $A_2^{\text{VII}}B_2^{\text{VII}}X_7$ . The weberite structure can be described as a network of corner-shared  $BX_6$  octahedra with the penetration of *A* cations (see Fig. 1). There are two types of  $BX_6$  octahedra: *B*-1 ( $B^{2+}$  in the case of  $A_2B^{2+}B^{3+}F_7$ ,  $A = \text{Na}^+$  or  $\text{Ag}^+$ ) in 4*c* Wyckoff positions, and *B*-2 ( $B^{3+}$  in the case of  $A_2B^{2+}B^{3+}F_7$ ) in 4*b* Wyckoff positions. Each of the six vertices of *B*-1 octahedra connects to another *B* octahedron, while only four vertices of a *B*-2 octahedron link to other *B* octahedra. The two unpaired vertices are in a *trans* configuration. As will be

discussed later, trigonal or monoclinic weberite variants cause a *cis* configuration (see Fig. 2). The *B*-1 octahedra are cornerlinked to each other and form *B*-1 octahedral chains parallel to the *A*1 chains (in the [100] direction). The *B*-2 octahedra are isolated from each other and link the *B*-1 octahedral chains to form a three-dimensional octahedral network.

The arrangements of A and B ions lead to three different cation tetrahedra. Six anions occupy the two  $A_3B$  ( $A_3BX$ , X1) and four  $A_2B_2$  tetrahedral interstices ( $A_2B_2X$ , X2) and none are located inside the two  $AB_3$  sites ( $AB_3$ ], where [] represents a vacant site) in a formula unit. The remaining anion (X3) maintains four coordination and lies outside the two edge-shared  $AB_3$  tetrahedra, very close to the shared B-B edge (see Fig. 3). X3 can also be considered to sit inside the octahedron  $(A_4B_2)$ , which shares faces with two adjacent  $AB_3$  tetrahedra, and distort towards the *B*-*B* edge (Grey *et al.*, 2003).

The weberite structure can also be considered as a stacking of repeated layers or slabs. The most common way to examine the structure is to view it as stacked, alternating close-packed metal layers  $A_3B$  and  $AB_3$  on (011) parallel planes. In  $A_3B$ layers, four A-1 and two A-2 ions form a hexagonal ring with B-2 occupying the center. In other words the A cations form Kagomé-type networks. [Kagomé in Japanese means a bamboo-basket woven pattern. It is formed by interlaced triangles and each lattice point has four equivalent bonds. 'Kagomé' was introduced by Husimi after he and his co-



Figure 1

*B*-octahedral network and *A* cations (*a*) in the [1, 0.04, 0.07] direction and (*b*) in the [0.1, 0, 1] direction; the black lines are the unit cell.



## Figure 2

(a) A B-1 octahedron in the center and its connection to another six octahedra; (b) *trans* configuration of B-2 octahedra; (c) *cis* configuration of B-2 octahedra.

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worker Syôzi found a new antiferromagnetic lattice by star-totriangle transformation from a honeycomb lattice (Mekata, 2003). Syôzi published the first Kagomé paper in 1951 (Syozi, 1951); see Fig. 4.] In  $AB_3$  layers the  $BX_6$  octahedron arrangement is nearly identical with the basal plane of the hexagonal tungsten bronze (HTB) structures and A-2 cations are in the center of the hexagonal rings. The HTB-like layers can also be simplified by a Kagomé net representation (Fig. 5). The HTB-like layers are displaced with respect to each other by an interlayer stacking vector (SV) which is defined as the projected distance, viewed down the (pseudo-) sixfold axis, between crystallographically similar ions in adjacent layers. White (1984) and Cohelho *et al.* (1997) used SV as an alternative description for zirconolite, zirkelite, pyrochlore and polymignyte. Here, SV is used to describe weberite. The stacking vectors in the weberite structure are nearly in the  $[0\bar{1}1]$ ,  $[\bar{3}1\bar{1}]$  and  $[31\bar{1}]$  directions. They are typically of the order 4 Å. The angle between successive stacking vectors (SA) is approximately 120°. The distance between two neighboring HTB-like layers along the (pseudo-) sixfold axis is approximately 5.8 Å. Fig. 6 shows the stacking vectors between three sequences of HTB layers.

There is yet another way to consider the weberite repeated layers. The first layer is formed by the alternating B-1 octahedral chains and A-1 distorted cube (or square prism) chains, which are in the [100] direction for classic orthorhombic weberites. In this layer the B-1 octahedra are edge-shared with



**Figure 3** Anion coordination: (a) X-1 in  $A_3B$ ; (b) X-2 in  $A_2B_2$ ; (c) X-3 in  $A_4B_2$ .



#### Figure 4

(a) Kagomé net presentation of A cations on  $A_3B$  layers; (b)  $AX_8$  polyhedral representation of  $A_3B$  layers, which are parallel to the (011) plane.

A-1 cubes. The second layer is alternating *B*-2 octahedra and A-2 bi-hexagonal pyramids in the [100] direction as in Fig. 7 (Rossell, 1979; Renaudin *et al.*, 1988).

## 2.2. Relationship to fluorite and pyrochlore

Weberite and pyrochlore  $(A_2B_2X_7)$  are both fluorite-related  $(AX_2 \text{ or } A_4X_8)$  superstructures. The coordination number of A and B is the same in both structures. These two structures have a similar cationic sublattice, which is comprised of stacked cubic close-packed cation layers, the same as (111) planes in fluorite. These layers alternate between the compositions  $A_3B$  and  $AB_3$  and are parallel to (111) planes in pyrochlore and



Figure 5

(a) Kagomé net presentation of B cations on  $AB_3$  layers; (b)  $BX_6$  polyhedral representation of  $AB_3$  layers, which are parallel to the (011) plane.

(011) planes in weberite.  $AB_3$  layers in pyrochlore can also be described as HTB-like layers. The length of SV and the value of SA of the pyrochlore structure are almost the same as weberite. However, the difference between the weberite and the pyrochlore structures is the different stacking of two successive  $AB_3$  and  $A_3B$  layers, which will be discussed later in this section. The crystallographic relationship between the weberite and the pyrochlore structures is further confirmed by the fact that the space group of weberite (*Imma*) is a subgroup of  $Fd\bar{3}m$ , the space group of pyrochlore. If the lattice parameter of pyrochlores is 2a with respect to fluorite a ( $a \simeq 5$  Å), then the lattice parameters of the classic orthorhombic



#### Figure 6

Left: Stacking vectors (black arrows) between three sequences of HTB layers; right: Kagomé nets of three successive HTB layers (purple arrows are stacking vectors). This figure is in color in the online version of this paper.





(a) The layer consisting of A1 and B1 lines; (b) A-2 and B-2 layers, viewed in the [010] direction.

Table 2					
Pyrochlore $(A_2B_2X_6X')$	) structure	data ii	1 space	group	Imcm.

			Atomic position					
Atoms Wyckoff position		Site symmetry	x	у	z			
Α	4 <i>b</i>	2/ <i>m</i>	0	0.5	0			
	4 <i>c</i>	2/ <i>m</i>	0.25	0.25	0.25			
В	4a	2/ <i>m</i>	0	0	0			
	4d	2/ <i>m</i>	0.25	0.75	0.25			
Χ	4 <i>e</i>	mm2	0.5	x + 0.25	0.25			
	4 <i>e</i>	mm2	0	x	0.25			
	16 <i>j</i>	1	x - 0.125	0.125	x + 0.125			
X'	4 <i>e</i>	mm2	0.25	0.375	0			

The x is the oxygen parameter inside the  $A_2B_2$  tetrahedral site. The value is between 0.3125 and 0.375.



# Figure 8

(a) Cationic network on (111) of fluorite; (b)  $AB_3$  layer; (c)  $A_3B$  layer on (011) of weberite; dashed lines are the unit cell; (d) axial transformation of pyrochlore to weberite [black dashed lines: a fluorite cell; blue lines: double pyrochlore cells; red dotted lines: weberite lattice; green shadow (011)<sub>w</sub> and (111)<sub>p</sub>]. This figure is in color in the online version of this paper.

weberites are approximately  $2^{1/2}a$ , 2a and  $2^{1/2}a$ . The rotation of  $45^{\circ}$  about the *b* axis of the pyrochlore cation sublattice leads to the weberite-like cation sublattice (Fig. 8). The (111) planes of pyrochlore are transformed to the (011) of the new lattice. The transformation relationship can be written as

$$W = P \begin{pmatrix} 0.5 & 0 & 0.5 \\ 0 & 1 & 0 \\ -0.5 & 0 & 0.5 \end{pmatrix}.$$
 (1)

The transformation leads to the space group *Imcm*, which is a different setting of *Imma*. The *Imma* lattice can be achieved by the  $90^{\circ}$  rotation of the coordinate system of *Imcm*. The transformation matrix is

 $\begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix}.$  (2)

The resulting lattice parameters in *Imma* are 2a,  $2^{1/2}a$  and  $2^{1/2}a$ . In order to match the weberite lattice parameters, the space group *Imcm* is preferred when presenting the atomic positions of pyrochlore in the weberitelike orthorhombic lattice (Table 2).

It is easy to recognize weberite and distinguish the three structures from powder diffraction. As is well known, in Cu Ka radiation to  $2\theta \simeq 70^\circ$ , the five fluorite characteristic peaks are (111), (200), (220), (311) and (222). The (111) reflection is at  $2\theta \simeq 30^\circ$  with the highest intensity. In pyrochlore, owing to the doubling of the lattice parameter with respect to fluorite, the five fluorite peaks become (222), (400), (440), (622) and (444). The appearance of several weak reflections, especially the (111) peak at  $2\theta \simeq 15^\circ$ , is a major difference between the X-ray diffraction (XRD) patterns of fluorite and pyrochlore. In orthorhombic weberite, the five fluorite peaks are split, for example, the most intense  $(111)_{f}$ or  $(222)_p$  are split into  $(022)_w$  and (220)<sub>w</sub>. There are several more reflections in weberite, which are systematic absences in pyrochlore, for example, (101)<sub>w</sub> and  $(020)_{\rm w}$  [corresponding to  $(200)_{\rm p}$ ]. Details on the XRD reflection for fluorite, pyrochlore and

weberite are listed in Table 3. For space reasons, only reflections up to  $(222)_{\rm f}$  are presented.

It is important to recall that in fluorites, each anion is at the center of the cationic tetrahedra  $(A_4X)$ . The arrangement of A and B leads to different cation tetrahedra:  $AB_3$ ,  $A_3B$  and  $A_2B_2$ in weberites, and  $A_4$ ,  $B_4$  and  $A_2B_2$  in pyrochlores. The reason for the formation of different cation tetrahedra is that weberites and pyrochlores are different in stacking two neighboring  $AB_3$  and  $A_3B$  layers, although generally they follow the pattern of cubic close-packed cation layers. The three nearest-neighbor metal ions in these layers form pseudoequilateral triangles. The distribution of A and B cations in  $AB_3$  layers will lead to two types of triangles:  $AB_2$  and  $B_3$ . The cations in the following  $A_3B$  layer lie above the centers of these triangles. If an  $AB_3$  layer is a reference, there are  $2^{1/2}a/2$ along  $[100]_{\rm w}$  or  $[10\overline{1}]_{\rm P}$  displacement in the above  $A_3B$  layer between weberite and pyrochlore. As a result, in the  $A_3B$ layer, A cations are above the center of  $AB_2$  triangles and B cations are above  $B_3$  triangles in pyrochlore, while in weberite, 2/3 A (A-1) and all B cations are above the AB<sub>2</sub> triangles and the remaining A cations (A-2) are above  $B_3$  triangles (see Fig. 9). Therefore, these arrangements lead to two  $AB_3$ , two  $A_3B$ and four  $A_2B_2$  in a formula unit of weberite, and in the case of pyrochlore, one  $A_4$ , six  $A_2B_2$  and one  $B_4$ . In addition, different stacking of two neighboring  $AB_3$  and  $A_3B$  layers can explain why the transformation of the pyrochlore cation sublattice into a weberite-like lattice results in a different setting of the space group.

As stated in §2.1, in a formula unit the X3 anion of weberite is located outside the cation tetrahedra and leaves two  $AB_3$ tetrahedra with a vacant center. In contrast, all anions in the pyrochlore structure are inside the cation tetrahedra. Therefore, it can be argued that pyrochlore is more closely related to fluorite than weberite since the former preserves all the anions in cation tetrahedral interstices (Yakubovich et al., 1993; Grey et al., 2003). In weberite it is understandable that the X-deficient site is more favorable in B-rich tetrahedra ( $AB_3$  than  $A_2B_2$  and  $A_3B$ ), because B ions have a smaller coordination number (CN). However, it raises the question: why there are two  $AB_3$  tetrahedra with a vacant center and the X3 is not inside the cation tetrahedra? Grey et al. (2003) argued that in  $Ca_2Ta_2O_7$  weberite, the sum of valence  $(\sum v/CN)$  in CaTa<sub>3</sub> tetrahedra is so highly over-saturated that CaTa<sub>3</sub> cannot accommodate X3. Actually, the highly over-saturated  $AB_3$ tetrahedra occur in all weberite compounds:  $A_2^{1+}B^{2+}B^{3+}F_7$ ,  $A_2^{2+}B_2^{5+}O_7$  and  $A_2^{1+}B_2^{6+}O_7$ . The nominal sum of valence in the center of  $AB_3$  is 1.46 for  $A_2^{1+}B^{2+}B^{3+}F_7$ , 2.75 for  $A_2^{2+}B_2^{5+}O_7$ , 3.13 for  $A_2^{1+}B_2^{6+}O_7$ . Thus, anions should distort largely towards A cations to meet the required valence, which would then result in a shorter A - X distance than a B - X distance. However, A ions are larger and have a larger CN than B ions and so the A - X bond length should be larger than the B - Xbond length. The end result is that anions cannot move towards A cations and the required valence cannot be achieved. By contrast, the sum of valence in the center of  $AB_3$ is under-saturated, being 0.875 for  $A_2^{1+}B^{2+}B^{3+}F_7$ , 1.58 for  $A_2^{2+}B_2^{5+}O_7$  and 1.375 for  $A_2^{1+}B_2^{6+}O_7$ . Anions are required to

#### Table 3

XRD reflections for fluorite, pyrochlore and weberite.

VDD	
хкр	гепест

XRD reflecti	ons			
hkl	hkl		hkl	Corresponding
(fluorite)	(pyrochlore)		(weberite)	pyrochlore plane
· · · · ·	,		. ,	
	111		011	111
		Į	101	200
		ι	020	020
		ſ	002	202
	220	{	121	220
		l	200	202
		ſ	112	311
	311	{	211	311
		l	031	131
111	222	ſ	022	222
111		l	220	222
200	400	ſ	202	400
200	400	l	040	040
		ſ	013	313
	331	{	132	331
		l	231	331
		ſ	103	402
			222	420
		Í	301	$40\overline{2}$
		l	141	240
		ſ	123	422
		ł	042	242
		l	321	$42\overline{2}$
			240	$24\overline{2}$
	333		033	333
		ſ	213	511
	511	ł	312	511
		l	051	151
		(	004	404
220	440	ł	242	440
		l	400	$40\bar{4}$
		ſ	114	513
			233	531
	504		152	351
	531	í	332	531
			251	351
		l	411	513
		(	024	424
			143	442
	442	í	341	$44\overline{2}$
		l	420	$42\overline{4}$
		ſ	303	600
		{	060	060
		(	204	602
	( <b>a</b> .)		323	620
	620	í	402	$60\overline{2}$
		l l	161	260
		(	134	533
	533	Į	053	353
		l	431	533
		(	224	622
			062	262
311	622	ſ	422	$62\overline{2}$
		l	260	262
		,	044	444
222	444	{	440	444

move towards B cations, which is favored by the bond length argument above. As for  $A_2B_2$  tetrahedra, the sum of valence is 1.08 for  $A_2^{1+}B^{2+}B^{3+}F_7$ , 2.17 for  $A_2^{2+}B_2^{5+}O_7$  and 2.25 for  $A_2^{1+}B_2^{6+}O_7$ . In this case the sum of valence is close to the anion oxidation state.

In order to check the stability of the X3, the empirical equation by Brese & O'Keeffe (1991) is used to calculate the valence of the X3

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$$V_i = \sum v_{ij} = \sum \exp((R_{ij} - r_{ij})/b)$$
 (3),

where  $R_{ij}$  is the bond-valence parameter,  $r_{ij}$  is the bond distance and b is a constant. Three representative compounds were chosen for detailed analysis:  $Na_2^{1+}Mg^{2+}Al^{3+}F_7$ ,  $Sr_2^{2+}Sb_2^{5+}O_7$  and  $Ag_2^{1+}Te_2^{6+}O_7$ . There are few, if any, reported bond-length data for  $Ag_2B_2F_7$ . Na<sub>2</sub>MgAlF<sub>7</sub> was chosen since it is the aristotype of the weberite compounds. The  $r_{ii}$  of  $Na_2^{1+}Mg^{2+}Al^{3+}F_7$  is from Knop *et al.* (1982) based on singlecrystal XRD.  $Sr_2^{2+}Sb_2^{5+}O_7$  was chosen because it is a stable weberite even under high pressure and neutron diffraction data are available (Knop et al., 1980; Groen & Ijdo, 1988). As for  $A_2^{1+}B_2^{6+}O_7$  compounds, only the crystal structure Ag<sub>2</sub>Te<sub>2</sub>O<sub>7</sub> has been reported (Klein et al., 2006). Table 4 lists the detailed valence information including all three anion types as well as cations by the empirical equation above using the bondvalence parameters (Brese & O'Keeffe, 1991; Brown, 2002) and the bond lengths  $(r_{ii})$  from the literature. The valence of X3 is close to its oxidation state in these compounds. It is worth noting that the discrepancy is small in  $Ag_2^{1+}Te_2^{6+}O_7$  for all three oxygen anions. Therefore,  $A_2^{1+}B_2^{6+}O_7$  weberites are possible.

Another significant difference is the formation of  $BX_6$ networks. All of the anions in weberites participate in the formation of  $BX_6$  octahedra, but only 6/7 of the anions in pyrochlores do. The  $BX_6$  octahedral network in both structures is fairly rigid. Therefore, in order to maintain the octahedral network it is difficult for the weberite to form vacancies at anion sites. By contrast, the pyrochlore structure tolerates Xdeficiency or paired A and X deficiencies relatively easily. Examples of such pyrochlore oxides are Bi<sub>1.5</sub>Zn<sub>0.92</sub>Nb<sub>1.5</sub>O<sub>6.92</sub> and Tl<sub>2</sub>B<sub>2</sub>O<sub>6</sub> (B = Nb, Ta and U), Tl<sub>2</sub>Os<sub>2</sub>O<sub>7-x</sub> and Pb<sub>2</sub>Os<sub>2</sub>O<sub>7-x</sub> (Nino, 2002; Subramanian *et al.*, 1983; Reading *et al.*, 2002). In addition, the substitution of small amounts of oxygen by F<sup>-</sup> may prevent the formation of weberites. For example, Ca<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub> pyrochlore transforms into weberite irreversibly



Figure 9

 $A_3B$  and  $AB_3$  slabs of (a) weberite and (b) pyrochlore. Cations connected by dotted lines are on the  $AB_3$  layer and by grey lines are on the  $A_3B$  layer. The red lines (or dotted line) show cation tetrahedra. This figure is in color in the online version of this paper.

$X1$ in $A_3B$ tetrahedra			$X2$ in $A_2B_2$	tetrahedra			X3 outside	the $AB_3$ tetral	hedra		
Bonds	$r_{ij}$ (Å)	V <sub>ij</sub>	$\sum v_{ij}$	Bonds	$r_{ij}$ (Å)	$v_{ij}$	$\sum v_{ij}$	Bonds	$r_{ij}$ (Å)	$v_{ij}$	$\sum v_{ij}$
Na <sub>2</sub> MgAlF	7										
Al-F	1.825	0.469		Mg-F	1.960	0.360		Mg-F	1.951	0.368	
Na2-F	2.211	0.236	0.072	Al-F	1.793	0.512	1.022	Mg-F	1.951	0.368	0.000
Na1-F	2.423	0.133	0.972	Na2-F	2.549	0.095	1.022	Na2-F	2.689	0.065	0.866
Na1-F	2.423	0.133		Na1-F	2.749	0.055		Na2-F	2.689	0.065	
Na1 <sup>1+</sup> : $\sum v_i$	j = 0.779; Na2	$1^{+}: \sum v_{ij} = 0.93$	81; $Mg^{2+}$ : $\sum v$	$_{ij} = 2.17; \text{ Al}^{3+}: \Sigma$	$v_{ij} = 2.89$						
Sr <sub>2</sub> Sb <sub>2</sub> O <sub>7</sub>											
Sb2-O	1.922	1.056		Sb1-O	1.971	0.926		Sb1-F	2.005	0.843	
Sr2–O	2.363	0.515	2 200	Sb2-O	2.202	0.512	0.151	Sb1-F	2.005	0.843	1.963
Sr1–O	2.502	0.354	2.280	Sr1-O	2.833	0.145	2.151	Sr2-F	2.850	0.138	
Sr1–O	2.502	0.354		Sr2-O	2.599	0.273		Sr2-F	2.850	0.138	
$\operatorname{Sr1}^{2+}: \sum v_{ij}$	$= 1.996; Sr2^{2+}$	$: \sum v_{ij} = 2.40;$	$\mathrm{Sb1}^{5+}:\sum v_{ij} =$	5.39; Sb2 <sup>5+</sup> : $\sum_{i}$	$v_{ij} = 5.34$						
Ag <sub>2</sub> Te <sub>2</sub> O <sub>7</sub>											
Te2-O	1.825	1.281		Ag1-O	2.806	0.067		Ag2-O	2.806	0.067	
Ag2–O	2.388	0.207	1.064	Ag2-O	2.549	0.134	2 0 11	Ag2-O	2.806	0.067	1 000
Ag1-O	2.465	0.168	1.864	Te1-O	1.997	0.806	2.041	Te1-O	1.946	0.925	1.983
Ag1-O	2.465	0.168		Te2-O	1.905	1.034		Te1-O	1.946	0.925	
$\operatorname{Ag1}^{1+}: \sum v_i$	$_{ij} = 0.939; Ag2$	<sup>1+</sup> : $\sum v_{ij} = 1.0$	84; Te1 <sup>6+</sup> : $\sum_{i}$	$v_{ij} = 5.785; \text{Te}2^{64}$	$\sum v_{ij} = 5.983$					-	

Examples of bond-valence sum for anions and cations by Brese and O'Keeffe.

 $r_{ij}$  is the bond distance,  $v_{ij}$  is the bond valence.

Table 4

above 973 K, but CaNaSb<sub>2</sub>O<sub>6</sub>F and Ca<sub>1.56</sub>Sb<sub>2</sub>O<sub>6.37</sub> $F_{0.44}$  pyrochlores are stable (Aleshin & Roy, 1962; Aia *et al.*, 1963).

## 2.3. Weberite-like structures

The weberite structures show a wide variety of different modifications including monoclinic and trigonal variants. Grev et al. (2003) proposed the use of the nomenclature of the International Mineralogical Association Commission New Minerals and Mineral Names (IMA-CNMMN), which was initially approved for zirconolite CaZrTi<sub>2</sub>O<sub>7</sub> (Bayliss et al., 1989). As discussed above, the basic building unit is a slab formed by one  $A_3B$  and one  $AB_3$  layer. The differences between weberites are the crystal system and the number of slabs (N) in a unit cell. A notation which combines N and the first letter of the crystal system is used to indicate different weberites. For example, the notation of the classic orthorhombic weberite is 20 because it has two slabs in a unit cell. The reported weberites include 20, 2M, 3T, 4M, 5M, 6M, 6T, 7*M* and 8*O*. Tables 5 and 6 list different types of  $A_2B_2F_7$  and  $A_2B_2O_7$  weberites, respectively. (NaCu)Cu<sub>2</sub>F<sub>7</sub> (or NaCu<sub>3</sub>F<sub>7</sub>, space group C2/c) and  $(Ca_{0.5}Ln_{1.5})(Ca_{0.5}Sb_{1.5})O_7$  (or  $CaLn_{1.5}Sb_{1.5}O_7$ , space group I2/m11, Ln = La, Pr, Nd and Y) are special 2M weberites and more like pseudo-2O weberites for they maintain the structural feature of 20 rather than 2M, as will be discussed later. Ca2Ta2O7-based compounds are important in the weberite family since for N > 4, only Ca2Ta2O7-based compounds have been reported. Grey and co-workers (Grey et al., 1999, 2001, 2003; Grey & Roth, 2000) have shown that  $Ca_2Ta_2O_7$  compounds can crystallize into 3T, 4M, 5M, 6T, 6M and 7M by different doping or synthesis methods and later Ebbinghaus et al. (2005) also synthesized an

 $8O \text{ Ca}_2\text{Ta}_2\text{O}_7$  single crystal using the optical floating zone method.

A significant difference between 20 and non-20 weberites is that the  $AB_3$  and  $A_3B$  layers are parallel to the (011) planes for 2O and parallel to the (001) planes for other weberites, except for NaCu<sub>3</sub> $F_7$  and CaLn<sub>1.5</sub>Sb<sub>1.5</sub>O<sub>7</sub> (Ln = La, Pr, Nd and Y). The formula unit (Z) of NaCu<sub>3</sub> $F_7$  and CaLn<sub>1.5</sub>Sb<sub>1.5</sub>O<sub>7</sub> is also consistent with 20 weberites, four rather than eight, the latter the formula unit for other 2M weberites. As in \$2.2 the lattice parameters of 2O weberites are approximately  $2^{1/2}a$ , 2a and  $2^{1/2}a$  ( $a \simeq 5$  Å, the lattice parameters for fluorite). The lattice parameters of 2M weberites are nearly  $6^{1/2}a$ ,  $2^{1/2}a$  and  $6^{1/2}a$ . The [011], [100] and [011] vectors of 2O become [100], [010] and [001] of 2M. The lattice parameter difference between 2M, 4M, 5M, 6M and 7M is mainly on the c axis. The lattice parameters for nM (n = 2, 4, 5 and 7) are approximately  $6^{1/2}a$ ,  $2^{1/2}a$  and  $[n(6)^{1/2}/2]a$  and they are nearly  $2^{1/2}a$ ,  $6^{1/2}a$  and 3(6)<sup>1/2</sup>/a for 6M (Grey et al., 1999, 2001, 2003; Grey & Roth, 2000). The 80 weberite is closely related to a monoclinic variant rather than 20 in both the orientation of the  $AB_3$  and  $A_3B$  layers and the lattice parameters. The lattice parameters are nearly  $2^{1/2}a$ ,  $6^{1/2}a$  and  $4(6)^{1/2}/a$ . As for 3T, the [100], [-0.5, -0.5, 0.5] and [012] vectors in 20 are transformed into the basal vectors. The resulting lattice parameters are approximately  $2^{1/2}a$ ,  $2^{1/2}a$  and  $2(3)^{1/2}a$ . The relationship of 2O, 2M and 3T weberites is shown in Fig. 10. Meanwhile, the lattice parameters of 6T are approximately  $2^{1/2}a$ ,  $2^{1/2}a$  and  $4(3)^{1/2}a$ , just double the length of the basal vector in the c axis.

For 2*O* weberites there are two special types in which the body-center symmetry is lost. The first case is when  $Cu^{2+}$  is introduced into  $Na_2B^{2+}B^{3+}F_7$  at *B*-1 sites such as  $Na_2CuCrF_7$ and  $Na_2CuInF_7$  (Kummer *et al.*, 1988; Ruchaud *et al.*, 1992). The common Jahn–Teller distortion (the CuF<sub>6</sub> octahedra are

# feature articles

## Table 5

List of  $A_2B_2F_7$  weberites.

		Space		Lattice para	meters						Properties
Туре		group	Ζ	a (Å)	b (Å)	c (Å)	eta (°)	$R_A$ (Å)	$R_B$ (Å)	$R_A/R_B$	investigated
20	Na <sub>2</sub> MgCrF <sub>7</sub> (Chassain, 1969)	Imma	4	7.39	7.15	10.20		1.18	0.667	1.768	
20	Na <sub>2</sub> MgGaF <sub>7</sub> (Chassain, 1969)	Imma	4	7.42	7.16	10.16		1.18	0.67	1.761	
20	Na <sub>2</sub> MgScF <sub>7</sub> (Chassain, 1969)	Imma	4	7.55	7.34	10.43		1.18	0.733	1.611	
20	Na <sub>2</sub> MgVF <sub>7</sub> (Chassain, 1969)	Imma	4	7.45	7.24	10.30		1.18	0.68	1.735	
20	Na <sub>2</sub> NiFeF <sub>7</sub> (Cosier <i>et al.</i> , 1970; Laligant <i>et al.</i> , 1989; Thompson <i>et al.</i> , 1992)	Imma	4	7.2338 (3)	10.3050 (3)	7.4529 (3)		1.18	0.62	1.903	Magnetic
20	Na <sub>2</sub> NiAlF <sub>7</sub> (Tressaud <i>et al.</i> , 1974; Heger, 1973)	Imma	4	7.31 (2)	7.07 (2)	10.04 (2)		1.18	0.603	1.959	Magnetic
20	Na <sub>2</sub> NiCoF <sub>7</sub> (Tressaud <i>et al.</i> , 1974; Cosier <i>et al.</i> , 1970)	Imma	4	7.40 (2)	7.20 (2)	10.24 (2)		1.18	0.618	1.911	Magnetic
20	Na <sub>2</sub> NiCrF <sub>7</sub> (Hansler & Rudorff, 1970; Laligant, Ferey <i>et al.</i> , 1987)	Ітта	4	7.183 (1)	10.224 (1)	7.414 (1)		1.18	0.653	1.808	Magnetic
20	Na <sub>2</sub> CoGaF <sub>7</sub> (Koch & Hebecker, 1988)	Ітта	4	7.3011 (6)	10.5436 (9)	7.3845 (7)		1.18	0.645	1.829	
20	Na <sub>2</sub> CoInF <sub>7</sub> (Koch & Hebecker, 1988)	Ітта	4	7.4032 (6)	10.3892 (8)	7.5302 (9)		1.18	0.745	1.5849	
20	Na <sub>2</sub> CoScF <sub>7</sub> (Koch & Hebecker, 1988)	Ітта	4	7.431 (1)	10.546 (1)	7.544 (1)		1.18	0.718	1.645	
20	Na <sub>2</sub> MnTIF <sub>7</sub> (Koch & Hebecker, 1988)	Ітта	4	7.371 (1)	10.369 (3)	7.603 (1)		1.18	0.67	1.761	
20	Na <sub>2</sub> NiGaF <sub>7</sub> (Koch & Hebecker, 1988; Dahlke <i>et al.</i> , 1998)	Ітта	4	7.1805 (7)	10.2433 (9)	7.4256 (7)		1.18	0.655	1.802	
20	Na <sub>2</sub> NiInF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.3632 (5)	10.3490 (7)	7.5274 (6)		1.18	0.745	1.584	
20	Na <sub>2</sub> NiScF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.3116 (7)	10.3278 (9)	7.4779 (7)		1.18	0.718	1.645	
20	Na <sub>2</sub> MgTIF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.3756 (8)	10.418 (1)	7.5496 (8)		1.18	0.695	1.698	
20	Na <sub>2</sub> ZnFeF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.281 (1)	10.446 (2)	7.459 (1)		1.18	0.645	1.829	
	Na <sub>2</sub> ZnGaF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.2494 (7)	10.3283 (8)	7.3582 (6)		1.18	0.68	1.735	
20	Na <sub>2</sub> ZnInF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.4077 (6)	10.4759 (9)	7.5732 (6)		1.18	0.77	1.532	
20	Na <sub>2</sub> ZnTIF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.338 (1)	10.300 (2)	7.539 (1)		1.18	0.705	1.674	
20	Na <sub>2</sub> MgFeF <sub>7</sub> (Pankhurst <i>et al.</i> , 1991; Chassain, 1969)	Imma	4	7.49	7.25	10.26		1.18	0.635	1.858	Magnetic
20	Na <sub>2</sub> MgAlF <sub>7</sub> (Byström, 1944; Knop et al., 1982)	Imma	4	7.501 (1)	9.968 (2)	7.285 (1)		1.18	0.618	1.911	
20	Na <sub>2</sub> ZnAlF <sub>7</sub> (Dahlke & Babel, 1994)	Ітта	4	7.092 (1)	10.092 (1)	7.337 (1)		1.18	0.6375	1.851	
20	Ag <sub>2</sub> CuMnF <sub>7</sub> (Koch & Hebecker, 1988)	Ітта	4	7.5006 (9)	10.5025 (9)	7.6452 (8)		1.28	0.655	1.954	
20	$Ag_2CoAlF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.252	10.16	7.601		1.28	0.603	2.124	
20	$Ag_2CoGaF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.313	10.35	7.678		1.28	0.655	1.954	
20	$Ag_2CoInF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.544	10.72	7.851		1.28	0.745	1.718	
20	$Ag_2CoScF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.497	10.64	7.789		1.28	0.718	1.784	
20	$Ag_2MnAlF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.360	10.32	7.601		1.28	0.593	2.160	
20	$Ag_2MnGaF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.465	10.62	7.787		1.28	0.645	1.986	
2O	$Ag_2MnScF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.634	10.78	7.802		1.28	0.708	1.809	
2O	$Ag_2NiGaF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.255	10.28	7.650		1.28	0.655	1.954	
20	$Ag_2NiScF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.463	10.54	7.771		1.28	0.718	1.785	
20	$Ag_2MgAlF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.197	10.01	7.571		1.28	0.618	2.073	
20	$Ag_2MgGaF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.257	10.21	7.664		1.28	0.67	1.910	
20	$Ag_2MgInF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.495	10.62	7.832		1.28	0.76	1.684	
20	$Ag_2MgScF_7$ (Koch <i>et al.</i> , 1982)	Imma	4	7.427	10.52	7.782		1.28	0.733	1.747	
20	Ag <sub>2</sub> CuAlF <sub>7</sub> (Koch et al., 1982)	Imma	4	7.109	10.22	7.684		1.28	0.623	2.056	
20	Ag <sub>2</sub> CuGaF <sub>7</sub> (Koch et al., 1982)	Imma	4	7.200	10.34	7.755		1.28	0.675	1.896	
20	$Ag_2ZnAlF_7$ (Koch et al., 1982)	Imma	4	7.237	10.14	7.590		1.28	0.6375	2.008	
20	Ag <sub>2</sub> ZnGaF <sub>7</sub> (Koch et al., 1982)	Imma	4	7.303	10.32	7.688		1.28	0.68	1.882	
20	Ag <sub>2</sub> ZnInF <sub>7</sub> (Koch et al., 1982)	Imma	4	7.531	10.71	7.841		1.28	0.77	1.662	
20	Ag <sub>2</sub> CoCrF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.349 (1)	10.376 (1)	7.683 (1)		1.28	0.653	1.962	
20	Ag <sub>2</sub> CoFeF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.3711 (8)	10.437 (1)	7.7145 (8)		1.28	0.62	2.065	
20	Ag <sub>2</sub> MnFeF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.490 (1)	10.612 (2)	7.731(1)		1.28	0.61	2.098	

# Table 5 (continued)

		Space		Lattice para	meters						Properties
Туре		group	Ζ	a (Å)	b (Å)	<i>c</i> (Å)	$\beta$ (°)	$R_A$ (Å)	$R_B$ (Å)	$R_A/R_B$	investigated
20	$Ag_2MnInF_7$ (Koch & Hebecker,	Imma	4	7.6747 (8)	10.856 (1)	7.8641 (7)		1.28	0.735	1.742	
20	$Ag_2MgCrF_7$ (Koch & Hebecker, 1988)	Imma	4	7.2746 (6)	10.3128 (9)	7.7060 (7)		1.28	0.668	1.918	
20	$Ag_2MgFeF_7$ (Koch & Hebecker, 1988)	Imma	4	7.3100 (7)	10.335 (1)	7.6972 (9)		1.28	0.635	2.016	
20	Ag <sub>2</sub> MgTIF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.2506 (9)	10.362 (2)	7.497 (1)		1.28	0.695	1.842	
20	Ag <sub>2</sub> CuCrF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.2103 (6)	10.454 (1)	7.7871 (8)		1.28	0.673	1.903	
20	$Ag_2CuFeF_7$ (Koch & Hebecker, 1988)	Imma	4	7.2435 (9)	10.474 (2)	7.769 (1)		1.28	0.64	2	
20	Ag <sub>2</sub> CuInF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.3461 (6)	10.7501 (9)	7.9098 (6)		1.28	0.765	1.673	
20	$Ag_2ZnCrF_7$ (Koch & Hebecker, 1988)	Imma	4	7.3165 (7)	10.362 (1)	7.6877 (8)		1.28	0.678	1.889	
20	Ag <sub>2</sub> ZnFeF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.359 (1)	10.409 (2)	7.706 (1)		1.28	0.645	1.985	
20	Ag <sub>2</sub> ZnMnF <sub>7</sub> (Koch & Hebecker, 1988)	Imma	4	7.408 (1)	10.503 (1)	7.6972 (9)		1.28	0.66	1.939	
20	Ag <sub>2</sub> NiAlF <sub>7</sub> (Dance et al., 1974)	Imma	4	7.564 (6)	7.210 (6)	10.139 (15)		1.28	0.603	2.124	Magnetic
20	Ag <sub>2</sub> NiCrF <sub>7</sub> (Dance et al., 1974)	Imma	4	7.673 (6)	7.305 (6)	10.285 (9)		1.28	0.653	1.962	Magnetic
20	Ag <sub>2</sub> NiFeF <sub>7</sub> (Dance et al., 1974)	Imma	4	7.692 (6)	7.345 (6)	10.345 (9)		1.28	0.62	2.065	Magnetic
20	Ag <sub>2</sub> NiInF <sub>7</sub> (Dance et al., 1974)	Imma	4	7.822 (6)	7.499 (6)	10.622 (9)		1.28	0.745	1.718	Magnetic
2 <i>O</i> -II	Na <sub>2</sub> CuInF <sub>7</sub> (Ruchaud et al., 1992)	Pmnb	4	7.318	10.602	7.712		1.18	0.765	1.542	Magnetic
2 <i>O</i> -II	Na <sub>2</sub> CuCrF <sub>7</sub> (Kummer et al., 1988;	Pmnb	4	7.100(1)	10.338 (1)	7.518 (1)		1.18	0.673	1.755	-
2 <i>O</i> -II	Koch & Hebecker, 1985) Na <sub>2</sub> CuScF <sub>7</sub> (Dahlke & Babel, $1004$ )	Pmnb	4	7.260 (1)	10.534 (1)	7.658 (1)		1.18	0.7375	1.6	
20.111	1994)	Duruh	4	7 256	10.224	7 502		1 10	0 745	1 501	Magnatia
20-III 20-III	Na <sub>2</sub> Nilli $F_7$ (Frenzen <i>et al.</i> , 1992) Na <sub>2</sub> MgIn $F_7$ (Caramanian <i>et al.</i> , 2001)	Pmnb Pnma	4	10.435 (1)	7.345 (1)	7.533 (1)		1.18	0.743	1.553	Magnetic
2M	Na <sub>2</sub> CuGaE <sub>7</sub> (Ruchaud <i>et al.</i> 1992)	C2/c	8	12,325 (5)	7.318 (1)	12,780 (5)	109.29(2)	1.18	0.675	1.748	Magnetic
2M and	Na <sub>2</sub> CuFeE <sub>7</sub> (Welsch & Babel 1992)	C2/c	8	12.323(3)	7 363 (8)	12.93(1)	109.29(2) 109.36(7)	1.10	0.64	1.844	magnetie
4 <i>M</i>	Yakubovich <i>et al.</i> , 1990; Kummer <i>et al.</i> , 1988)	C2/c	16	12.444 (2)	7.343 (1)	24.672 (5)	99.27 (3)	1.10	0.01	1.011	
3 <i>T</i>	Na <sub>2</sub> MnAlF <sub>7</sub> (Koch & Hebecker, 1988)		6	7.2854 (4)		17.844 (1)		1.18	0.593	1.992	
3 <i>T</i>	Na <sub>2</sub> MnInF <sub>7</sub> (Koch & Hebecker, 1988)		6	7.6006 (3)		18.617 (1)		1.18	0.735	1.605	
3 <i>T</i>	Na <sub>2</sub> MnScF <sub>7</sub> (Koch & Hebecker, 1988)		6	7.5442 (4)		18.479 (1)		1.18	0.708	1.668	
3 <i>T</i>	Na <sub>2</sub> MnGaF <sub>7</sub> (Courbion et al., 1988)	$P3_{1}21$	6	7.421 (3)		18.166 (6)		1.18	0.645	1.829	
3 <i>T</i>	Na <sub>2</sub> MnCrF <sub>7</sub> (Courbion <i>et al.</i> , 1988)	$P3_{1}21$	6	7.401 (1)		18.091 (2)		1.18	0.6425	1.837	
3 <i>T</i>	Na <sub>2</sub> MnVF <sub>7</sub> (Peschel & Babel, 1997)	<i>P</i> 3 <sub>1</sub> 21	6	7.467		18.216		1.18	0.655	1.802	
3 <i>T</i>	Na <sub>2</sub> MnFeF <sub>7</sub> (Verscharen & Babel, 1978; Cosier <i>et al.</i> , 1970; Boireau <i>et al.</i> , 1993)	<i>P</i> 3 <sub>1</sub> 21	6	7.488 (2)		18.257 (6)		1.18	0.61	1.934	Magnetic
3 <i>T</i>	$Ag_2MnInF_7$ (Koch & Hebecker, 1988)		6	7.751 (1)		18.838 (4)		1.28	0.735	1.741	
4 <i>M</i>	Na <sub>2</sub> CoAlF <sub>7</sub> (Boireau <i>et al.</i> , 1993; Gravereau <i>et al.</i> , 1992)	C2/c	16	12.378 (4)	7.210 (3)	24.019 (9)	99.67 (2)	1.18	0.613	1.927	Magnetic
4M	Na <sub>2</sub> ZnGaF <sub>7</sub> (Dahlke et al., 1998)	C2/c	16	12.519	7.303	24.353	99.74	1.18	0.68	1.735	
4M	Na <sub>2</sub> ZnFeF <sub>7</sub> (Dahlke et al., 1998)	C2/c	16	12.610	7.359	24.538	99.70	1.18	0.645	1.829	
4M	Na <sub>2</sub> FeVF <sub>7</sub> (Peschel et al., 1995)	C2/c	16	12.710 (3)	7.429(1)	24.716 (5)	100.03 (3)	1.18	0.625	1.888	
4M	Na <sub>2</sub> CoVF <sub>7</sub> (Peschel et al., 1995)	C2/c	16	12.703 (5)	7.391 (3)	24.651 (5)	100.02(3)	1.18	0.645	1.829	
4M	Na <sub>2</sub> FeCrF <sub>7</sub> (Peschel et al., 1995)	C2/c	16	12.625 (3)	7.391 (1)	24.695 (5)	99.93 (3)	1.18	0.6125	1.927	
4M	Na <sub>2</sub> Fe <sub>2</sub> F <sub>7</sub> (Yakubovich <i>et al.</i> , 1993; Cosier <i>et al.</i> , 1970; Tressaud <i>et</i>	C2/c	16	12.676 (3)	7.422 (1)	24.710 (5)	99.97 (3)	1.18	0.58	2.034	Magnetic
4M	Na <sub>2</sub> CoFeF <sub>7</sub> (Welsch & Babel, 1992; Cosier <i>et al.</i> , 1970; Tressaud <i>et</i>	C2/c	16	12.622 (10)	7.360 (4)	24.516 (20)	99.71 (5)	1.18	0.62	1.903	Magnetic
4M	<i>al.</i> , 1974; Boireau <i>et al.</i> , 1993) Na <sub>2</sub> CoCrF <sub>7</sub> (Boireau <i>et al.</i> , 1993;	C2/c	16	12.578 (3)	7.335 (1)	24.415 (5)	99.64 (3)	1.18	0.653	1.808	Magnetic
4 <i>M</i>	Peschel <i>et al.</i> , 1995) Na <sub>2</sub> FeAlF <sub>7</sub> (Dahlke <i>et al.</i> , 1998; Tressaud <i>et al.</i> , 1974)	C2/c	16	12.426	7.278	24.206	99.99	1.18	0.563	2.098	Magnetic

# Table 6

List of weberite oxides with  $R_A/R_B$  and the relative ionicity of the A-O bond.

		Lattice param	eters							Properties
Туре		a (Å)	b (Å)	<i>c</i> (Å)	$\beta$ (°)	$R_A$ (Å)	$R_B ({\rm \AA})$	$R_A/R_B$	$I_A/(I_B+I_A)$	investigated
20	Ca <sub>2</sub> Sb <sub>2</sub> O <sub>7</sub> (Bystrom, 1945; Ivanov et al., 1998; Sato et al., 2002; Lin et al. 2006)	7.28 7.3060 7.2900	7.44 7.4627 10.2000	10.18 10.2263 7.4500		1.12	0.6	1.86667	0.60636	Ferroelectric and photocatalytic
20	Cd <sub>2</sub> Sb <sub>2</sub> O <sub>7</sub> (Brisse <i>et al.</i> , 1972; Bystrom, 1945)	7.21	7.33	10.14		0.9	0.6	1.5	0.56093	photocatalytic
20	Sr <sub>2</sub> Sb <sub>2</sub> O <sub>7</sub> (Knop <i>et al.</i> , 1980; Groen & Ijdo, 1988; Lin <i>et al.</i> , 2006; Sato <i>et al.</i> , 2002)	7.452 7.4557 (2) 7.4557	7.687 10.3708 (3) 10.3708	10.381 7.6860 (1) 7.6860		1.26	0.6	2.1	0.61038	Ferroelectric and photocatalytic
20	Pb <sub>2</sub> Sb <sub>2</sub> O <sub>7</sub> (Ivanov & Zavodnik, 1990; Ivanov <i>et al.</i> , 1998)	7.484 (1) 7.4774	7.857 (1) 7.8549	10.426 (2) 10.4250		1.29	0.6	2.15	0.54792	Ferroelectric
20	Ca <sub>2</sub> Os <sub>2</sub> O <sub>7</sub> (Reading <i>et al.</i> , 2002; Weller <i>et al.</i> , 2003)	7.2104 (2)	10.1211 (3)	7.3813 (2)		1.12	0.575	1.94783	0.55518	Electronic
20	Sr <sub>2</sub> Bi <sub>2</sub> O <sub>7</sub> (Knop et al., 1980)	7.70	7.91	10.58		1.26	0.76	1.65789	0.58305	
20 20	Ba <sub>2</sub> U <sub>2</sub> O <sub>7</sub> (Cordfunke & Ijdo, 1988) Na <sub>2</sub> Te <sub>2</sub> O <sub>7</sub> (Knop & Demazeau, 1981)	8.1665 (15) 7.233 (5)	11.3081 (21) 10.104 (7)	8.1943 (16) 7.454 (5)		1.42 1.18	0.76 0.56	1.86842 2.10714	0.5232 0.64905	
20	$Ag_2Te_2O_7$ (Klein <i>et al.</i> , 2006)	7.266 (2)	10.1430 (9)	7.6021 (17)		1.28	0.56	2.28571	0.60811	Denne els stais
20 20	$DyNaSb_2O_7$ (Desgardin <i>et al.</i> , 1998) 1977)	7.26 (6)	7.3362	10.3521 10.20 (6)		1.205 1.1035	0.6	2.00833 1.83917	0.59219 0.6051	Ferroelectric
20	GdNaSb <sub>2</sub> O <sub>7</sub> (Desgardin <i>et al.</i> , 1977)	7.29 (1)	7.47 (0)	10.20 (7)		1.1165	0.6	1.86083	0.60468	
20	EuNaSb <sub>2</sub> O <sub>7</sub> (Desgardin <i>et al.</i> , 1977)	7.30 (0)	7.47 (2)	10.21 (4)		1.123	0.6	1.87167	0.6088	
20	SmNaSb <sub>2</sub> O7 (Desgardin <i>et al.</i> , 1977)	7.30 (8)	7.45 (7)	10.22 (7)		1.1295	0.6	1.8825	0.60636	
20	NdNaSb <sub>2</sub> O7 (Desgardin <i>et al.</i> , 1977)	7.32 (7)	7.49 (2)	10.24 (2)		1.1445	0.6	1.9075	0.60636	
20	$PrNaSb_2O_7$ (Desgardin <i>et al.</i> , 1977)	7.33 (7)	7.50 (6)	10.25 (5)		1.153	0.6	1.92167	0.58322	
20	LalvaSb <sub>2</sub> O <sub>7</sub> (Desgardin <i>et al.</i> , 1977) KLuSb <sub>2</sub> O <sub>7</sub> (Klein <i>et al.</i> , 2006; Sych, Kabanova & Andreeva, 1988; Sych, Kabanova, Garbuz & Kovalenko, 1988)	7.23	10.23	7.39		1.17 1.2435	0.6	2.0725	0.60759	
20	KYbSb <sub>2</sub> O <sub>7</sub> (Klein <i>et al.</i> , 2006; Sych, Kabanova & Andreeva, 1988; Sych, Kabanova, Garbuz & Kovalenko, 1988)	7.24	10.25	7.40		1.2475	0.6	2.07917	0.61077	
20	KErSb <sub>2</sub> O <sub>7</sub> (Klein <i>et al.</i> , 2006; Sych, Kabanova & Andreeva, 1988; Sych, Kabanova, Garbuz & Kovalenko, 1988)	7.26	10.25	7.41		1.257	0.6	2.095	0.6088	
20	KHoSb <sub>2</sub> O <sub>7</sub> (Klein <i>et al.</i> , 2006; Sych, Kabanova & Andreeva, 1988; Sych, Kabanova, Garbuz & Kovalenko, 1988)	7.26	10.25	7.42		1.2625	0.6	2.10417	0.6092	
20	KYSb <sub>2</sub> O <sub>7</sub> (Klein <i>et al.</i> , 2006; Sych, Kabanova & Andreeva, 1988; Sych, Kabanova, Garbuz & Kovalenko, 1988)	7.26	10.25	7.43		1.2645	0.6	2.1075	0.6088	
20	KYTa <sub>2</sub> O <sub>7</sub> (Gade & Chincholkar, 1979)	7.78	10.82	7.50		1.2645	0.64	1.97578	0.5324	
20	KDyTa <sub>2</sub> O <sub>7</sub> (Gade & Chincholkar, 1979)	7.80	10.88	7.70		1.2685	0.64	1.98203	0.53282	
20	KGdTa <sub>2</sub> O <sub>7</sub> (Gade & Chincholkar, 1979)	7.84	10.86	7.72		1.2815	0.64	2.00234	0.5324	
20	KSmTa <sub>2</sub> O <sub>7</sub> (Gade & Chincholkar, 1979)	7.86	10.82	7.76		1.2945	0.64	2.02266	0.53405	
20	NaDyV <sub>2</sub> O <sub>7</sub> (Gade & Chincholkar, 1979)	7.53	10.94	7.44		1.1035	0.54	2.04352	0.53496	
20	NaGdV <sub>2</sub> O <sub>7</sub> (Gade & Chincholkar, 1979)	7.56	10.88	7.46		1.1165	0.54	2.06759	0.54352	
20	NaSmV <sub>2</sub> O <sub>7</sub> (Gade & Chincholkar, 1979)	7.58	10.86	7.48		1.1295	0.54	2.09167	0.54526	
20	NaNdV <sub>2</sub> O <sub>7</sub> (Gade & Chincholkar, 1979)	7.62	10.82	7.50		1.1445	0.54	2.11944	0.54526	
20	NaSrSbTeO <sub>7</sub> (Burchard & Rudorff, 1979)	Not reported				1.22	0.58	2.10345	0.62891	

## Table 6 (continued)

		Lattice param	eters							Properties
Туре		a (Å)	b (Å)	c (Å)	$\beta$ (°)	$R_A ({\rm \AA})$	$R_B({\rm \AA})$	$R_A/R_B$	$I_A/(I_B+I_A)$	investigated
20	NaCdSbTeO <sub>7</sub> (Burchard & Rudorff, 1979)	Not reported				1.04	0.58	1.7931	0.60778	
20	NdCaSbTeO <sub>7</sub> (Burchard & Rudorff, 1979)	Not reported				1.15	0.58	1.9828	0.62694	
20	Na <sub>0.5</sub> Cd <sub>1.5</sub> (Fe <sub>0.5</sub> Te <sub>1.5</sub> )O <sub>7</sub> (Burchard & Rudorff, 1979)	7.131	7.317	10.183		1.12	0.5575	2.00897	0.59584	
20	Na <sub>0.5</sub> Ca <sub>1.5</sub> (Fe <sub>0.5</sub> Te <sub>1.5</sub> )O <sub>7</sub> (Burchard & Rudorff, 1979)	Not reported				1.135	0.5575	2.0358744	0.626874	
20	Ba <sub>0.5</sub> Ca <sub>1.5</sub> (Fe <sub>0.5</sub> Te <sub>1.5</sub> )O <sub>7</sub> (Burchard & Rudorff, 1979)	7.176	7.464	10.140		1.195	0.5725	2.08734	0.627674	
2M	CaLa <sub>1.5</sub> Sb <sub>1.5</sub> O <sub>7</sub> (Au et al., 2007)	7.5753 (3)	10.6870 (5)	7.5482 (3)	90.346 (3)	1.15	0.7	1.6428571	0.57329	
2M	$CaPr_{1.5}Sb_{1.5}O_7$ (Au <i>et al.</i> , 2007)	7.5188 (3)	10.6111 (4)	7.4952 (2)	90.315 (2)	1.1245	0.7	1.6064286	0.569502	
2M	$CaNd_{1.5}Sb_{1.5}O_{7}$ (Au <i>et al.</i> , 2007)	7.5019 (2)	10.5890 (3)	7.4770 (2)	90.298 (2)	1.11175	0.7	1.5882143	0.569502	
2M	$CaY_{1,5}Sb_{1,5}O_{7}$ (Au <i>et al.</i> , 2007)	7.3905 (1)	10.4563 (2)	7.3894 (1)	90.049 (1)	1.04425	0.7	1.4917857	0.55821	
3 <i>T</i>	Ca <sub>1.5</sub> Mn <sub>0.5</sub> Sb <sub>2</sub> O <sub>7</sub> (Bonazzi & Bindi, 2007)	7.282 (2)		17.604 (4)		1.04	0.6	1.73333	0.59369	
3 <i>T</i>	Mn <sub>2</sub> Sb <sub>2</sub> O <sub>7</sub> (Scott, 1990)	7.191		17.402		0.96	0.6	1.6	0.540094	
3 <i>T</i>	Ca <sub>1.92</sub> Ta <sub>1.92</sub> Nd <sub>0.08</sub> Zr <sub>0.08</sub> O <sub>7</sub> (Grey <i>et al.</i> , 2003)	7.356 (1)		18.116 (1)		1.11956	0.61728	1.8136988	0.529853	
3 <i>T</i>	Ca <sub>2</sub> Ta <sub>2</sub> O <sub>7</sub> (Cava <i>et al.</i> , 1998; Grey <i>et al.</i> , 1999)	7.355 (1)		18.09 (1)		1.12	0.64	1.75	0.52985	Dielectric
4M	Ca <sub>1.92</sub> Ta <sub>1.92</sub> Nd <sub>0.08</sub> Zr <sub>0.08</sub> O <sub>7</sub> (Grey <i>et al.</i> , 2003)	12.761 (1)	7.358 (1)	24.565 (1)	100.17	1.12	0.64	1.75	0.52922	
5 <i>M</i>	Ca <sub>1.8</sub> Ta <sub>1.8</sub> Sm <sub>0.24</sub> Ti <sub>0.17</sub> O <sub>7</sub> (Grey & Roth, 2000)	12.763 (1)	7.130 (1)	30.190 (1)	94.09 (1)	1.13635	0.62743	1.81113	0.52523	
5 <i>M</i>	$Ca_{2}Ta_{1,8}Nb_{0,2}O_{7}$ (Grev <i>et al.</i> , 2001)	12.749 (1)	7.347 (1)	30.23 (1)	94.23 (1)	1.12	0.64	1.75	0.52866	Dielectric
6M	$Ca_2Ta_2O_7$ (Grey <i>et al.</i> , 1999)	7.348 (3)	12.727 (3)	36.44 (5)	95.9 (1)	1.12	0.64	1.75	0.52985	
6 <i>T</i>	Ca <sub>1.89</sub> Ta <sub>1.86</sub> Sm <sub>0.16</sub> Ti <sub>0.1</sub> O <sub>7</sub> (Grey & Roth, 2000)	7.353 (1)		36.264 (1)		1.1792	0.63505	1.85686	0.52649	
7M	Ca <sub>2</sub> Ta <sub>1.9</sub> Nb <sub>0.1</sub> O <sub>7</sub> (Grey <i>et al.</i> , 2001)	12.714 (1)	7.370(1)	42.45 (1)	95.75 (1)	1.12	0.64	1.75	0.52925	Dielectric
80	Ca <sub>2</sub> Ta <sub>2</sub> O <sub>7</sub> (Ebbinghaus et al., 2005)	7.3690 (2)	12.7296 (3)	48.263 (1)		1.12	0.64	1.75	0.52985	Dielectric and optical

R is the ionic radius from Shannon (1976),  $\chi$  is the electronegativity from Allred & Rochow (1958), I is the bond ionicity.

elongated perpendicular to the B-1 chains) in CuF<sub>6</sub> octahedra leads to the lowering of symmetry, while maintaining the orthorhombic lattice. The space group is reduced to Pmnb, a subgroup of Imma (Yakubovich et al., 1993). Another case of losing *I*-centering symmetry happens when the ionic radius of B-2 is larger than that of B-1. In a classic 20 weberite structure the ionic radius of B-2 is equal to or smaller than that of B-1. When a larger B-2 ion appears in a weberite compound, the anions, which are shared by two B-1 octahedral neighbors, distort toward B-2 ions. As a result, the A-2 ions cannot hold eight-coordination and change to seven-coordination. The B-2 ion keeps octahedral coordination with a seventh anion relatively close to it. As in the case of Na<sub>2</sub>NiInF<sub>7</sub>, the distance between the distorted anion and B-2 (In<sup>3+</sup>) is only 1.3 times larger than the shortest In-F bond length in B-2 octahedra (Frenzen et al., 1992). In a 20 weberite structure, the ratio of the two distances is higher, such as 1.97 in Na<sub>2</sub>MgAlF<sub>7</sub> or 1.83 in Ca<sub>2</sub>Os<sub>2</sub>O<sub>7</sub> (Wyckoff, 1963; Reading et al., 2002). The distortion of the anion excludes the I-centering of the structure and results in the space group Pnmb (Yakubovich et al., 1993). The notation of 20-II and 20-III is used for the first and the second condition, respectively.

One extreme case for 2*O*-III is  $Ln_2(B,Ln)O_7$  (or  $Ln_3BO_7$ , where  $Ln^{3+}$  is a rare-earth element, and *B* is  $Os^{5+}$ ,  $Re^{5+}$ ,  $Ru^{5+}$ ,  $Re^{5+}$ ,  $Mo^{5+}$ ,  $Ir^{5+}$ ,  $Sb^{5+}$ ,  $Nb^{5+}$  or  $Ta^{5+}$ ). *B*-2 ions are the same as *A* ions. As a result, the *B*-2 sites and *A*-2 sites are indistinguishable. The structure has an arrangement of  $BO_6$ – $LnO_8$  layers (much like weberites), but a different cation configuration with VII coordination between the layers (Fig. 11). Due to the fact that this type of structure does not maintain the three-dimensional  $BO_6$  octahedral network, it is considered a weberite-type structure rather than the weberite structure, or sometimes it is reported as a La<sub>3</sub>NbO<sub>7</sub>-type structure (Rossell, 1979; Allpress & Rossell, 1979; Rooksby & White, 1964; Abe et al., 2004, 2006; Cai & Nino, 2007; Cai et al., 2007; Wakeshima et al., 2004; Groen et al., 1987; Wakeshima & Hinatsu, 2006; Nishimine et al., 2007; Gemmill et al., 2007; Khalifah et al., 1999, 2000; Wiss et al., 2000; Bontchev et al., 2000; Harada & Hinatsu, 2001; Harada et al., 2001; Nishimine et al., 2005; Gemmill et al., 2004, 2005; Vanberkel & Ijdo, 1986; Kahnharari et al., 1995; Wltschek et al., 1996; Greedan et al., 1997; Lam et al., 2002; Plaisier et al., 2002; Lam et al., 2003; Barrier & Gougeon, 2003; Hinatsu et al., 2004; Vente & Ijdo, 1991). Table 7 lists examples of  $Ln_3BO_7$  and their properties that have been investigated. Details on the dielectric properties of Ln<sub>3</sub>NbO<sub>7</sub> have been reported and will be covered in §3.2.2.

There is a special type of weberite  $(B^{+2}B^{+3}F_5\cdot 2H_2O)$  named inverse weberite (please see Table 7 for examples). In this structure *A* cations are missing. In order to maintain charge neutrality, two H<sub>2</sub>O molecules take the place of two F<sup>-</sup> ions. This structure has the same characteristic *B* octahedral network, just like the 2*O* weberite structure. The space group and Wyckoff positions of *B* cations and anions are the same as in the 2*O* weberite. However,  $B^{2+}$  ions take *B*-2 sites while  $B^{3+}$  cations lie at *B*-1 sites in this structure, which is opposite to the classic weberite structure (Laligant, Calage *et al.*, 1986; Laligant, Leblanc *et al.*, 1986; Laligant, Pannetier *et al.*, 1986; Laligant, Pannetier *et al.*, 1987; Weil & Werner, 2001; Leroux *et al.*, 1995; Subramanian *et al.*, 2006).

The investigation of  $Na_2B^{2+}B^{3+}F_7$  weberites indicates that the resulting structure type is determined by the size of the  $B^{2+}$ 



#### Figure 10

(a) Relationship between 20, 2M and 3T weberites (origin at the A2 site); large spheres: A ions; small spheres: B ions; blue solid lines: multiple unit cells of 2O; red dotted lines: the unit cell of 2M; green dashed lines: the unit cell of 3T. (b) (001) plane of 3T (green dashed lines) and 2M [red dotted lines, also indicating (011) of 2O].

cations. With increasing ionic radius of  $B^{2+}$ , the structure changes from 2*O* to 2*M*, 4*M* and to 3*T*, gradually (Yakubovich *et al.*, 1993). As for oxide weberites, it is clear that the *A* cation still plays an important role, for example, 2*O* Ca<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub>, 3*T* Ca<sub>1.5</sub>Mn<sub>0.5</sub>Sb<sub>2</sub>O<sub>7</sub> and 3*T* Mn<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub> (Ivanov *et al.*, 1998; Bonazzi & Bindi, 2007; Scott, 1990; Butler *et al.*, 1950; Bystrom, 1945). The occurrence of the monoclinic and trigonal variants may be closely related to the ionic radius ratio of the *A* and *B* cations. However, due to the limited number of compounds reported in each weberite-like structure, it is difficult to define the factors that determine when the variants occur.

As discussed before, the unpaired vertex (terminal anions) of *B*-2 octahedra are in *trans* configurations in 2*O* weberites. The trigonal and monoclinic variants produce another type of *B*-2 octahedra with the *cis* configuration (see Figs. 2*b* and *c*). Grey and co-workers (Grey & Roth, 2000; Grey *et al.*, 2003) figured out that the relative position of the terminal anions is a characteristic of weberite polytypes. In 2*M* and 3*T* polytypes *cis-B*2 are only in  $A_3B$  layers, while *trans-B*2 are only in  $AB_3$  layers (Grey *et al.*, 2003; Yakubovich *et al.*, 1993). The 4*M* and 6*T* weberites have alternative *cis* and *trans* configurations in successive  $A_3B$  layers (Grey & Roth, 2000; Grey *et al.*, 2003).

Several research groups (Yakubovich *et al.*, 1993, 1990; Dahlke *et al.*, 1998; Verscharen & Babel, 1978; Welsch & Babel, 1992) proposed that the formation of *B*-1 chains is a characteristic of  $Na_2B^{2+}B^{3+}F_7$  weberite polytypes. The detailed description about the different stacking sequence and the orientation of *B*-1 chains in 2O, 2M, 3T and 4M variants has been reported by Yakubovich *et al.* (1993). Here, the discussion is expanded to include all 2O, 2M, 3T, 4M, 5M, 6M, 6T, 7M and 8O variants. There are three different orientations for *B*-1 chains: type  $\alpha$ , type  $\beta$  and type  $\gamma$ . These three orientations are correlated with each other by a threefold rotation.



#### Figure 11

Weberite-type  $Ln_3BO_7$ , viewed in the [0.05, 0.05, 1] direction. The layers of  $LnO_8$  and  $BO_6$  lines are parallel to the (001) plane. Between the layers are Ln with a coordination number of 7.

#### Table 7

Examples of weberite-type Ln<sub>3</sub>BO<sub>7</sub> and inverse weberites.

		Space		Lattice param	neters		Properties	
Туре	Compounds	group	Ζ	a (Å)	b (Å)	<i>c</i> (Å)	investigated	
Weberite type	La <sub>3</sub> NbO <sub>7</sub> (Abe <i>et al.</i> , 2004, 2006; Allpress & Rossell, 1979)	Стст	4	11.167 (1)	7.629 (1)	7.753 (1)	Dielectric and photocatalytic	
Weberite type	La <sub>3</sub> TaO <sub>7</sub> (Allpress & Rossell, 1979; Abe <i>et al.</i> , 2004, 2006)	Стст	4	11.1863 (4)	7.6152 (3)	7.7556 (3)	Catalytic and magnetic	
Weberite type	Pr <sub>3</sub> NbO <sub>7</sub> (Vente et al., 1994)	Cmcm	4	10.959(1)	7.5240 (7)	7.6676 (7)	Magnetic	
Weberite type	Pr <sub>3</sub> TaO <sub>7</sub> (Vente et al., 1994)	Cmcm	4	10.973 (1)	7.5230 (7)	7.6721 (7)	Magnetic	
Weberite type	Nd <sub>3</sub> NbO <sub>7</sub> (Cai <i>et al.</i> , 2007; Allpress & Rossell, 1979)	Стст	4	10.905 (2)	7.517 (2)	7.624 (1)	Dielectric	
Weberite type	Gd <sub>3</sub> NbO <sub>7</sub> (Cai <i>et al.</i> , 2007; Allpress & Rossell, 1979; Astafyev <i>et al.</i> , 1985)	C222 <sub>1</sub>	4	10.610 (1)	7.521 (1)	7.550 (1)	Dielectric	
Weberite type	Gd <sub>3</sub> TaO <sub>7</sub> (Wakeshima et al., 2004)	C221 <sub>1</sub>	4	10.6259 (4)	7.5234 (3)	7.5446 (3)	Magnetic	
Weberite type	Dy <sub>3</sub> TaO <sub>7</sub> (Wakeshima et al., 2004)	C222 <sub>1</sub>	4	10.5332 (3)	7.4447 (2)	7.4816 (2)	Magnetic	
Weberite type	Ho <sub>3</sub> TaO <sub>7</sub> (Wakeshima et al., 2004)	$C222_{1}$	4	10.4873 (4)	7.4292 (3)	7.4499 (3)	Magnetic	
Inverse	$Fe_2F_5(H_2O)_2$ (Laligant, Pannetier et al., 1986; Greneche et al., 1988; Hall et al., 1977)	Imma	4	7.447 (1)	10.8623 (2)	6.652 (1)	Magnetic	
Inverse	ZnFeF <sub>5</sub> (H <sub>2</sub> O) <sub>2</sub> (Laligant, Calage <i>et al.</i> , 1986)	Imma	4	7.475 (1)	10.766 (1)	6.594 (1)	Magnetic	
Inverse	MnFeF <sub>5</sub> (H <sub>2</sub> O) <sub>2</sub> (Laligant, Calage et al., 1986; Laligant, Pannetier et al., 1987; Greneche et al., 1988)	Imma	4	7.5635 (2)	10.901 (1)	6.7319 (3)	Magnetic	
Inverse	MnAlF <sub>5</sub> (H <sub>2</sub> O) <sub>2</sub> (Subramanian <i>et al.</i> , 2006)	Imma	4	7.229 (2)	10.487 (4)	6.816 (2)		
Inverse	MgAlF <sub>5</sub> (H <sub>2</sub> O) <sub>2</sub> (Subramanian <i>et al.</i> , 2006; Weil & Werner, 2001)	Imma	4	7.057 (2)	10.125 (4)	6.798 (2)	Electrical resistivity	
Inverse	MnVF <sub>5</sub> (H <sub>2</sub> O) <sub>2</sub> (Subramanian <i>et al.</i> , 2006; Leroux <i>et al.</i> , 1995)	Imma	4	7.607 (2)	10.912 (4)	6.728 (2)	Magnetic	

For 2*O* weberites (including 2*O*-II and 2*O*-III), the stacking sequence of *B*-1 chains is  $\alpha\alpha\alpha$ ... (the orientation is parallel to the [100] direction). The same applies for pseudo-2*O* NaCu<sub>3</sub>F7 and CaLn<sub>1.5</sub>Sb<sub>1.5</sub>O<sub>7</sub> (Ln = La, Pr, Nd and Y), special cases of 2*M* (Renaudin *et al.*, 1988; Au *et al.*, 2007). The directions of the *B*-1 chains for 2*M* (except NaCu<sub>3</sub>F<sub>7</sub> and CaLn<sub>1.5</sub>Sb<sub>1.5</sub>O<sub>7</sub>) and 4*M* weberites are either nearly parallel to [110] (type  $\beta$ ) or [ $\overline{110}$ ] (type  $\gamma$ ). The stacking array for 2*M* is  $\beta\gamma\beta\gamma$ , while it is  $\beta\beta\gamma\gamma\beta\beta\gamma\gamma$  for the 4*M* polytype. As for 3*T* and 6*T*, the directions of the *B*-1 chains are nearly parallel to [010], [100] or [110]. The sequence of *B*-1 chains is  $\alpha\beta\gamma$  in 3*T* and  $\alpha\alpha\beta\beta\gamma\gamma\alpha\alpha\beta\gamma\gamma$  in 6*T* weberites.

It is important to note that the close-packed cation layers are stacked the same as f.c.c. (face-centered cubic: cubic stacking in which the stacking sequence is ABCABC...) in 20, 2M, 3T, 4M and 6T polytypes. The cation layers in 5M, 6M, 7M and 8O polytypes (Ca<sub>2</sub>Ta<sub>2</sub>O<sub>7</sub>-based compounds) are a mixture of cubic stacking and hexagonal stacking. The hexagonal stacking layers act as mirror glide planes for the cations, for example, the stacking sequence of 5M is ABCACBACAB in a unit cell (the underline letters indicate a hexagonal stacking; Grey et al., 1999, 2001). Therefore, 5M, 6M, 7M and 80 polytypes are not pure weberite. The weberite blocks are separated by *h*-stacking layers. A simpler approach is to describe the stacking of c as cubic and h as hexagonal. The stacking sequence is ccchccchcc for 5M [simplified as (3c)h(3c)h(2c), the integers indicating the number of c stacking layers], (5c)h(5c)h for 6M, (5c)h(7c)h for 7M and (4c)h(7c)h(3c) for 80 (Ebbinghaus et al., 2005; Grey et al., 1999, 2001, 2003; Grey & Roth, 2000). There are several structural features resulting from the introduction of h stacking:

(i) h stacking only occurs in the CaTa<sub>3</sub> cation layers;

(ii) h stacking causes the appearance of B-3 octahedra on the CaTa<sub>3</sub> cation layers and the neighboring Ca<sub>3</sub>Ta cation layers, which have only one unpaired vertex (B-1 octahedra have no unpaired vertex and B-2 have two);

(iii) in h stacking layers B-3 chains are formed, but no B-1 chains.

In these cases type  $\alpha$  is nearly parallel to [100] for 8*O* or [010] for 5*M* and 7*M*. Type  $\beta$  is nearly parallel to [110] and type  $\gamma$  is nearly parallel to [ $\overline{1}10$ ]. The directions of the *B* chains are  $\beta \beta \alpha \gamma \gamma$  for 5*M*,  $\gamma \beta \gamma \beta \gamma \beta$  for 6*M*,  $\gamma \alpha \gamma \alpha \beta \alpha \beta$  for 7*M* and  $\alpha \overline{\beta} \alpha \gamma \alpha \beta \alpha \gamma$  for 8*O* (*B*-3 chains are underlined). In summary, the stacking sequence of *B* chains changes with different weberite variants (see Fig. 12) and the formation of *B* chains is a characteristic of all weberites.

## 2.4. Stability field

Both pyrochlores and weberites have  $BX_6$  octahedral networks. Owing to the fact that *B*-2 octahedra have two unpaired vertices, the  $BX_6$  octahedral network in weberite is typically less compact. Therefore, weberite has more potential to permit larger radii of *A* ions. Fig. 13 shows a diagram of  $R_A$  versus  $R_B$  for 159 pyrochlore oxides and 131 weberite compounds (83 weberite fluorides and 48 weberite oxides, see Tables 5 and 6 for a complete list and references). The 159

pyrochlore oxides are taken from two articles (Subramanian *et al.*, 1983; Isupov, 2000). Fig. 13 indicates that the majority of pyrochlores have  $R_A$  ranging from 0.97 to 1.13 Å, while most weberites have  $R_A$  values ranging from 1.10 to 1.30 Å.

Weberite  $Ba_2U_2O_7$  has the highest  $R_A$  value of 1.42 Å (Cordfunke & Ijdo, 1988; Shannon, 1976). This clearly shows that larger  $R_A$  values prefer the formation of the weberite (Brisse *et al.*, 1972). The ratio of  $R_A/R_B$  for the weberite is



## Figure 12

*B* chains in different weberite-like structures. The vectors across the octahedra indicate the orientations of the *B* chains. (a) 20, (b) 2M, (c) 3T, (d) 4M, (e) 5M, (f) 6T, (g) 6M, (h) 7M and (i) 8O.

between 1.5 and 2. The two end-members are  $Cd_2Sb_2O_7$  and  $Ag_2Te_2O_7$ . However, the range of  $R_A/R_B$  for weberite greatly overlaps with the stability field for pyrochlore: 1.46–1.8 for  $A_2^{3+}B_2^{4+}O_7$  and 1.4–2.2 for  $A_2^{2+}B_2^{5+}O_7$  (Subramanian *et al.*, 1983). Therefore, the ionic radius ratio is not the only determining factor in the structural stability.

Electronegativity  $(\chi)$  is another important factor in the field of existence, because the formation of weberites is closely related to the covalent character of the bonds (Svch, Kabanova, Garbuz et al., 1988; Lopatin et al., 1985; Weller et al., 2003; Burchard & Rudorff, 1979). Weller et al. (2003) used only  $\chi_A$  and  $\chi_B$  to picture the stability field of the weberite, but their study only included a limited number of compounds. Lopatin et al. (1982, 1985) successfully utilized  $\chi_A$  and  $R_A/R_B$ to distinguish pyrochlores and weberites, and  $\chi_B$  and  $R_A/R_B$  to determine the different regions of the weberite and the layered perovskite. They chose Allred-Rochow (Allred & Rochow, 1958) electronegativities (which were completed by Little & Jones, 1960) because Allred-Rochow electronegativities are more precise when measuring the degree of covalent character of the bonds. Sych et al. (Sych, Kabanova, Garbuz et al., 1988) introduced  $R_A/R_B$  versus the relative ionicity of the A-O bond, which is the ratio of the ionicity of the A - O bond to the sum of the ionicity of the A - O and B - OO bonds. The ionicity of the A-O bond is calculated as

$$I_{A-O} = 1 - \exp[-0.25(\chi_A - \chi_O)^2].$$
 (4)

They used the electronegativities for the crystalline state calculated by Batanov (1975). The advantage of relative ionicity is that it contains the information for both A-O and B-O bonds. Therefore, the relative ionicity of A-O versus  $R_A/R_B$  is used to determine the stability field in this study, as shown in Fig. 14. Here, the electronegativities of Allred-Rochow (Allred & Rochow, 1958) and Little-Jones (Little & Jones, 1960) were used in calculating the ionicity. In Fig. 14(*a*) there is no obvious separation between weberites and pyrochlores. The reason for this may be that both  $A_2^{2+}B_2^{5+}O_7$  and  $A_2^{3+}B_2^{4+}O_7$  pyrochlore compounds are plotted. There are very



#### Figure 13

Summary of  $R_A$  versus  $R_B$  for weberites (including oxide and fluorine) and pyrochlore oxides.

few, if any,  $A_2^{3+}B_2^{4+}O_7$  weberites reported. Most weberites are  $A_2^{2+}B_2^{5+}O_7$  or  $(A, A')_2^{2+}(B, B')_2^{5+}O_7$  and several  $A_2^{1+}B_2^{6+}O_7$  (Na<sub>2</sub>Te<sub>2</sub>O<sub>7</sub> and Ag<sub>2</sub>Te<sub>2</sub>O<sub>7</sub>). The inclusion of  $A_2^{3+}B_2^{4+}O_7$ , particularly high-pressure phases, complicates the stability field, therefore, Fig. 14(*b*) only contains  $A_2^{2+}B_2^{5+}O_7$ ,  $(A, A')_2^{2+}(B, B')_2^{5+}O_7$  compounds Na<sub>2</sub>Te<sub>2</sub>O<sub>7</sub> and Ag<sub>2</sub>Te<sub>2</sub>O<sub>7</sub> (all weberites points in Fig. 14(*b*), there is a clear separation between weberites and pyrochlores. The dashed line is for visual effect – above the line is the weberite region. Weberites prefer a higher ratio of  $I_{A-O}/(I_{A-O} + I_{B-O})$  and a higher ratio of  $R_A/R_B$  than pyrochlores.

It is worth mentioning four specific compounds: Cd<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub>  $(R_{Cd^{2+}} = 0.9 \text{ Å})$  in the pyrochlore region, and Ca<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub>,  $Ca_2Os_2O7 (R_{Ca^{2+}} = 1.12 \text{ Å}) \text{ and } Pb_2Sb_2O_7 (R_{Pb^{2+}} = 1.29 \text{ Å}) \text{ in}$ the weberite region (Shannon, 1976). A high-pressure study has been performed on the first three compounds to investigate the transformation of the pyrochlore and weberite phases. Cd<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub> can form a metastable phase of weberite, which can be fully converted to pyrochlore under high pressure. Ca<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub> weberite is more stable than Cd<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub> weberite. The same high-pressure condition only results in mixed phases of Ca<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub> pyrochlore and weberite (Knop et al., 1980). At one atmosphere, Ca<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub> crystallizes as a pyrochlore below 973 K, above which it transforms to a weberite (Brisse et al., 1972). Meanwhile, Ca2Os2O7 weberite is stable and the synthesis of pyrochlore Ca<sub>2</sub>Os<sub>2</sub>O<sub>7</sub> under pressure leads to calcium-deficient Ca1.7Os2O7 (Reading et al., 2002; Weller et al., 2003). The reported crystal structure of Pb<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub> also strongly depends on the synthesis conditions. Low-temperature firing or wet chemical synthesis resulted in a



Stability field for weberite.

cubic pyrochlore phase. The cubic phase was metastable and readily transformed into weberite or rhombohedrally distorted pyrochlore (Ivanov *et al.*, 1998; Brisse *et al.*, 1972). These four compounds can crystallize as different polymorphs depending on the processing history, as presented in Fig. 14(b). It is worth noting that although the ionic radii ratio and bond ionicity are two major factors, there may be some additional crystallochemical characteristics or parameters that play a role in determining the prevalence of weberite over pyrochlore or *vice versa*. It would be interesting to perform some computational calculations (*e.g.* density functional theory) to shed light on the comparative lattice energy and stability field of pyrochlore and weberite.

# 3. Interesting properties and potential applications

For fluorine-based weberites, the magnetic properties attract most of the attention. The triangular network formed by  $B^{2+}$  and  $B^{3+}$  cations in the HTB-like planes generally support three different magnetically ordered systems:

(i) the diamagnetic  $B^{3+}$  ions separate linear chains of paramagnetic  $B^{2+}$  ions, for example, antiferromagnetic Na<sub>2</sub>NiAlF<sub>7</sub>, Na<sub>2</sub>FeAlF<sub>7</sub> and Na<sub>2</sub>NiInF<sub>7</sub> (Frenzen *et al.*, 1992; Heger, 1973);

(ii) both  $B^{2+}$  and  $B^{3+}$  are paramagnetic ions, like ferromagnetic Na<sub>2</sub>NiFeF<sub>7</sub> and antiferromagnetic Na<sub>2</sub>NiCrF<sub>7</sub> (Laligant *et al.*, 1989; Thompson *et al.*, 1992; Heger, 1973; Frenzen *et al.*, 1992);

(iii) diamagnetic  $B^{2+}$  forming linear chains which isolate the paramagnetic  $B^{3+}$  such as antiferromagnetic Na<sub>2</sub>MgFeF<sub>7</sub> (Pankhurst *et al.*, 1991).

As for weberite oxide, various properties have been investigated including the photocatalytic properites (Abe et al., 2004, 2006; Sato et al., 2002; Lin et al., 2006), the resistivity of Ca<sub>2</sub>Os<sub>2</sub>O<sub>7</sub> weberite (Reading et al., 2002), magnetic properties (Khalifah et al., 1999; Wakeshima et al., 2004; Wakeshima & Hinatsu, 2006), ferroelectric properties (Ivanov et al., 1998; Astafev et al., 1985) and dielectric properties (Cai & Nino, 2007; Cava et al., 1998; Grey et al., 2001). The interest in the properties is first due to the fact that the weberite structure is considered more favorable for the realisation of a ferroelectric state than the pyrochlore structure (Astafev et al., 1985). The Sb-based compounds are the most investigated weberites for ferroelectric properties. Ten years ago, Cava et al. (1998) found that the temperature coefficients of the dielectric constant  $(TC\varepsilon_r)$  of the Ca<sub>2</sub>Ta<sub>2</sub>O<sub>7</sub>-Ca<sub>2</sub>Nb<sub>2</sub>O<sub>7</sub> system can be close to zero. A series of investigations on Ca2Ta2O7-based weberites have followed (Grev et al., 1999, 2001, 2003; Grev & Roth, 2000; Ebbinghaus *et al.*, 2005).  $Ln_3BO_7$  (where Ln = rare-earthelements and B is Nb or Ta) are also interesting weberite-type compounds. The crystal structure is related to the ionic radius of Ln<sup>3+</sup>, which provides a stage for the study of structuredielectric properties relationships. This section will focus on the ferroelectric properties and dielectric properties of weberite oxides.

# 3.1. Ferroelectric properties

 $A_2$ Sb<sub>2</sub>O<sub>7</sub> ( $A = Ca^{2+}$ , Pb<sup>2+</sup> and Sr<sup>2+</sup>) are perhaps the most studied weberites owing to their ferroelectric properties. Second-harmonic generation and heat-capacity measurements indicated a possible ferroelectric phase transition in Pb<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub>. Dielectric constants showed a thermal hysteresis around the Curie temperature  $(T_c)$  in Pb<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub> (Astafev *et al.*, 1985; Milyan & Semrad, 2005). Single-crystal X-ray and powder neutron diffraction were performed in detailed crystallographic studies (Ivanov & Zavodnik, 1990; Astafev et al., 1985). Below  $T_c$ , there is a slight distortion from a centrosymmetric structure and ionic displacements cause spontaneous polarization in this structure. The results indicated a non-centrosymmetric (space group I2cm) to centrosymmetric (space group Imam, another setting of Imma) phase transition (Astafev et al., 1985; Ivanov et al., 1998; Ivanov & Zavodnik, 1990).  $T_c$  depends on the A cation: 510 K for Pb<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub>,110 K for Ca<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub> and 90 K for Sr<sub>2</sub>Sb<sub>2</sub>O<sub>7</sub>. The substitution of Ca by Pb in  $Ca_2Sb_2O_7$  causes a shift of  $T_c$  towards a higher temperature: 200 K for CaPbSb<sub>2</sub>O<sub>7</sub> weberite. Therefore, the A sublattice seems more likely to be the ferroelectrically active one

It is worth noting that  $Pb_2Sb_2O_7$  can also form rhombohedrally distorted pyrochlore (Brisse *et al.*, 1972). The pyrochlore phase is paraelectric even at room temperature. Actually,  $Pb_2Sb_2O7$  weberite has a higher  $T_c$  than most Pbbased pyrochlores. These facts may serve as evidence that the weberite structure is more suitable for the appearance of the ferroelectric state (Astafev *et al.*, 1985; Isupov, 2000).

# 3.2. Dielectric properties

3.2.1. Ca2Ta2O7-based compounds. According to Grey and co-workers (Grey *et al.*, 1999) the structure of pure  $Ca_2Ta_2O_7$ is 3T weberite up to 1673 K, where it transforms to the 7Mpolytype. The structure can be easily modified by doping and different synthesis routines (Grey et al., 1999, 2001, 2003; Grey & Roth, 2000; Ebbinghaus et al., 2005). One of the most interesting dielectric properties of Ca2Ta2O7 is that the temperature coefficient of the dielectric constant  $(TC\varepsilon_r)$  is 0 when mixing with 18 mol% of Ca<sub>2</sub>Nb<sub>2</sub>O<sub>7</sub>, meeting the requirement for the application of microwave dielectrics (Cava *et al.*, 1998).  $TC\varepsilon_r \simeq 0$  can be easily understood because  $TC\varepsilon_r$  is negative for Ca<sub>2</sub>Ta<sub>2</sub>O<sub>7</sub> (-444 p.p.m. K<sup>-1</sup> at 295 K) and positive for Ca<sub>2</sub>Nb<sub>2</sub>O<sub>7</sub> (231 p.p.m. K<sup>-1</sup> at 295 K). Extensive studies on the structure of the  $(1 - x)Ca_2Ta_2O_{7-x}Ca_2Nb_2O_7$ system have been performed by powder and single-crystal Xray diffraction, and powder neutron diffraction (Grey et al., 2001). The system forms 7M weberite solid solutions up to x =0.1 and Ca<sub>2</sub>Nb<sub>2</sub>O<sub>7</sub>-type solid solutions from x = 0.2-1. When x = 0.1, the structure transforms into 5*M*. The solubility limit is reached when the substitution of Ca<sub>2</sub>Nb<sub>2</sub>O<sub>7</sub> increases to 15 mol% and Ca2Nb2O7 forms as a second phase. The presence of Ca<sub>2</sub>Nb<sub>2</sub>O<sub>7</sub> thus results in  $TC\varepsilon_r$  compensation, making it approximately zero.

Another interesting aspect is that most of the  $(1-x)Ca_2Ta_2O_{7-x}Ca_2Nb_2O_7$  compounds have higher dielec-

Structural	comparison	of	three	weberite-type	structures	(Allpress	&
Rossell, 19	79; Rossell,	1979	9).				

	La <sub>3</sub> NbO <sub>7</sub>	Nd <sub>3</sub> NbO <sub>7</sub>	Gd <sub>3</sub> NbO <sub>7</sub>
$\Delta d_{\text{Ln}-\text{O}}/(d_{\text{Ln}-\text{O}})_{\text{av}}$ in LnO <sub>8</sub> cube	13.33	7.14	13.06
Deviation of O-Ln-O angle from perfect cube (°)	-9.87-6.46	-2.37-2.47	-5.77-8.88
$\Delta d_{\rm Nb-O}/(d_{\rm Nb-O})_{\rm av}$ in NbO <sub>6</sub> octa- hedra (%)	1.64	0.41	4.86
Deviation of O-Nb-O angle from perfect octahedra	-1.58-1.58	0.27-0.42	-5.63-5.63

 $d_{\rm Ln-O}$  and  $d_{\rm Nb-O}$  represents the bond length between  ${\rm Ln}^{3+}$  and  ${\rm O}^{2-}$  and the bond length between  ${\rm Nb}^{5+}$  and  ${\rm O}^{2-}$ , respectively.  $\Delta d_{\rm Ln-O}$  means the difference of longest and shortest bond length between  ${\rm Ln}^{3+}$  and  ${\rm O}^{2-}$  in  ${\rm LnO}_8$  distorted cubes.  $\Delta d_{\rm Nb-O}$  is the difference of the longest and shortest bond length between  ${\rm Nb}^{5+}$  and  ${\rm O}^{2-}$  in  ${\rm NbO}_6$  distorted octahedra.  $(d_{\rm Ln-O})_{\rm av}$  is the average bond length between  ${\rm Ln}^{3+}$  and  ${\rm O}^{2-}$  in  ${\rm LnO}_8$  distorted cubes.  $(d_{\rm Nb-O})_{\rm av}$  is the average bond length between  ${\rm Nb}^{5+}$  and  ${\rm O}^{2-}$  in  ${\rm NbO}_6$  distorted octahedra.

tric constants (above 30) than pure Ca<sub>2</sub>Ta<sub>2</sub>O<sub>7</sub> and Ca<sub>2</sub>Nb<sub>2</sub>O<sub>7</sub> at 1 MHz (Cava et al., 1998). However, another set of published dielectric constants of 5M  $Ca_2Ta_{1.8}Nb_{0.2}O_7$  and 7M Ca<sub>2</sub>Ta<sub>1.9</sub>Nb<sub>0.1</sub>O<sub>7</sub> are approximately 18 and 20 at 1 MHz, respectively, which are lower than the previous publication (Grey et al., 2001). It is not clear what causes the discrepancy in dielectric constant measurement. It may be due to different firing conditions and measurement methods. Dielectric properties at radio frequency have also been investigated. The dielectric constants of 3T Ca<sub>1.6</sub>Nd<sub>0.4</sub>Ta<sub>1.6</sub>Zr<sub>0.4</sub>O<sub>7</sub>, 5M Ca<sub>2</sub>Ta<sub>1.8</sub>Nb<sub>0.2</sub>O<sub>7</sub> and 7M Ca<sub>2</sub>Ta<sub>1.9</sub>Nb<sub>0.1</sub>O<sub>7</sub> are approximately stable (18-19) from 100 kHz up to 5 GHz and reach a maximum (22, 24.5 and 26.1, respectively) at  $\sim 8$  GHz. The dielectric constant is comparable for some important microwave dielectrics, such as  $BaMg_{1/3}Ta_{2/3}O_3$  (~24; Reaney & Iddles, 2006). However, the problem with these systems is that they have low quality factors ( $Q \simeq 200$ ) for technical applications (Grey et al., 2001).

It is interesting to see that 8*O* Ca<sub>2</sub>Ta<sub>2</sub>O<sub>7</sub>, which is synthesized by the optical floating zone melting method from 3*T* Ca<sub>2</sub>Ta<sub>2</sub>O<sub>7</sub> powder, has a relatively high dielectric constant (~ 60) at room temperature (Ebbinghaus *et al.*, 2005). And  $\varepsilon_r$ increases to 90 at 50 K. The high dielectric constant may result from a net dipole created by the off-center Ta<sup>5+</sup> in the TaO<sub>6</sub> octahedra of the Ca<sub>3</sub>Ta layers. The shifting of Ta<sup>5+</sup> also produces two short Ta–O bonds and two long Ta–O bonds, leading to the distortion of TaO<sub>6</sub> octahedra. The high dielectric constant and the ability to tailor it are interesting for scientific study and possible electronic applications.

In addition, the crystallographic study of  $Nd_2Zr_2O_7$  and  $Sm_2Ti_2O_7$  doping  $Ca_2Ta_2O_7$  has been conducted by Grey *et al.* (Grey *et al.*, 2003; Grey & Roth, 2000). The resulting phases include 3*T*, 4*M*, 5*M* and 6*T* weberites. The great structural flexibility of  $Ca_2Ta_2O_7$ -based compounds is interesting in a crystallographic study and may have potentials in technical applications.

**3.2.2.** Weberite-type  $Ln_3NbO_7$ . As stated in §2.3,  $Ln_2(Nb,Ln)O_7$  (or  $Ln_3NbO_7$ , where Ln is  $La^{3+}$ ,  $Pr^{3+}$ ,  $Nd^{3+}$  and  $Gd^{3+}$ ) is a weberite-type structure. It is an extreme case of 2*O*-

III weberite structure, in which A-2 and B-2 are the same. Our recent study on the dielectric properties of  $Ln_3NbO_7$  (Ln = La<sup>3+</sup>, Nd<sup>3+</sup> and Gd<sup>3+</sup>) showed some interesting results (Cai et al., 2007; Cai & Nino, 2007). As shown in Fig. 15, all three compounds exhibited a dielectric relaxation behavior similar to that observed in pyrochlore compounds (Roth et al., 2008; Nino et al., 2001). The permittivity increases sharply with increasing temperature until a maximum is reached. After that, the permittivity decreases slightly with an increase in temperature. The permittivity is between 35 and 60 for La<sub>3</sub>NbO<sub>7</sub> and 34-47 for Gd<sub>3</sub>NbO<sub>7</sub> from 113 to 473 K, and is between 34 and 62 for Nd<sub>3</sub>NbO<sub>7</sub> from 113 to 673 K at 1 MHz. These three compounds have close permittivity at 113 K. The relaxation temperatures are different, 183, 473 and 323 K for La<sub>3</sub>NbO<sub>7</sub>, Nd<sub>3</sub>NbO<sub>7</sub> and Gd<sub>3</sub>NbO<sub>7</sub>, respectively. The difference in relaxation temperature indicates the possibility of tailoring the temperature at which dielectric relaxation occurs through variations in compositions. As for the origin of different dielectric relaxation temperatures, a possible explanation is provided by comparing the structure. The main difference between the structure is that in Gd<sub>3</sub>NbO<sub>7</sub> the polyhedra are more distorted (Wakeshima et al., 2004; Allpress & Rossell, 1979; Rossell, 1979). In Table 8 polyhedral distortions are quantified in the deviation of bond length and bond angle. The calculation is based on the atomic positions after Rossell (1979). Nd<sub>3</sub>NbO<sub>7</sub> has nearly perfect NbO<sub>6</sub> octahedra, while Gd<sub>3</sub>NbO<sub>7</sub> has the most distorted octahedra. The LnO<sub>8</sub> cube in Nd<sub>3</sub>NbO<sub>7</sub> is the least distorted while LaO<sub>8</sub> and GdO<sub>8</sub> cubes have comparable distortion. These distortions are attributed to the 'openness' of the structure which causes an easier polarization of the material and results in a lower relaxation temperature (Astafyev et al., 1985). Additional details on the relationship of dielectric relaxation and polyhedral distortions are ongoing and will be a matter for future publications.

Owing to the interesting dielectric loss behavior observed in  $Gd_3NbO_7$  its characterization includes more frequencies (1, 4, 6, 10, 30, 80, 100, 300, 800 kHz and 1 MHz), as shown in Fig. 15(c). The temperature ( $T_m$ ), at which the loss peak occurs increases with increasing measuring frequency. To better understand the phenomena, the Arrhenius function is used to model the relaxation behaviour of  $Gd_3NbO_7$ 

$$v = v_0 \exp\left(-\frac{E_{\rm a}}{k_{\rm B}T_{\rm m}}\right),\tag{5}$$

where v is the measuring frequency, the pre-exponential  $v_0$  is the attempt-jump frequency,  $E_a$  is the activation energy and  $k_B$ is Boltzmann's constant.  $T_m$  is determined for each measuring frequency by fitting the loss peak to a Gaussian function. The non-symmetric tails of loss peaks are cut off during fitting. The resulting Arrhenius plot is presented in Fig. 15(*d*). From the linear fit,  $v_0 = 1.51 \times 10^{11}$  Hz, and the activation energy  $E_a$  is 0.45 eV, which is larger than typical values observed in Nbbased pyrochlores, for example 0.32 eV in Ca–Ti–Nb–O pyrochlore and 0.14 eV in Bi–Zn–Nb–O pyrochlore (Roth *et al.*, 2008; Nino, 2002). However, other ionic and dipolar compounds systems have even higher activation energies; for example, 0.53 eV for CaF<sub>2</sub>-doped NaF and 1.02 eV for (Ba<sub>0.8</sub>Sr<sub>0.2</sub>)(Ti<sub>1-x</sub>Zr<sub>x</sub>)O<sub>3</sub> (Johnson *et al.*, 1969; Cheng *et al.*, 2004). Thus, the calculated  $E_a$  is acceptable.

The dielectric study of  $Ln_3NbO_7$  compounds points to the possibility of tailoring the dielectric relaxation and develop further a paradigm for the compositional design of fluorite-related ceramics with optimized dielectric properties.

# 4. Conclusions

There are a considerable number of weberite compounds  $(A_2B_2X_7)$  that have been studied to date. Here the stability field in terms of the ratio of  $R_A$  and  $R_B$ , and the relative bond ionicity has been established. This structure can be interpreted in different ways. As an anion-deficient fluorite structure, it has similar close-packed cationic networks as fluorite and pyrochlore. It is presented here that the cation sublattices of the weberite and the pyrochlore structures are correlated by an axial transformation and that the different stacking inside

an  $AB_3$  and  $A_3B$  cation slab leads to a different coordination environment of anions in weberite and pyrochlore. There are various types of weberite-like structures. They can be distinguished by the number of  $AB_3$  and  $A_3B$  slabs and the crystal system. *B* chains are a characteristic of all weberite structures even for weberite polytypes with N > 4. The stacking sequence and the orientation of *B*-chains changes with respect to monoclinic and trigonal variants.

So far, investigations have primarily focused on the crystallographic aspects of weberites and some weberite compounds are reported to have interesting properties. It is clear that they are of great scientific interest. However, few studies have concentrated on the properties and possible applications. There is no doubt that weberite compounds possess various useful properties that can be tailored owing to the fact that many metal cations can be introduced into this structure as well as that a large diversity of variants exist in this structure. The realisation of the potential of weberites for electrical applications will grow as more extensive studies are conducted and knowledge of the structures increases.





Dielectric properties between 1 kHz and 1 MHz of (a) La<sub>3</sub>NbO<sub>7</sub>, (b) Nd<sub>3</sub>NbO<sub>7</sub>, (c) Gd<sub>3</sub>NbO<sub>7</sub> and (d) Arrhenius analysis of Gd<sub>3</sub>NbO<sub>7</sub>.

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